Method to Calibrate Fission Chambers in Campbelling Mode

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Method to calibrate fission chambers in Campbelling mode

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Abstract—Fission chambers are neutron detectors which are widely used to instrument experimental reactors such as material testing reactors or zero power reactors. In the presence of a high level mixed gamma and neutron flux, fission chambers can be operated in Campbelling mode (also known as “fluctuation mode” or “mean square voltage mode”) to provide reliable and precise neutron related measurements. Fission chamber calibration in Campbelling mode (in terms of neutron flux) is usually done empirically using a calibrated reference detector. A major drawback of this method is that calibration measurements have to be performed in a neutron environment very similar to the one in which the calibrated detector will be used afterwards. What we propose here is a different approach based on characterizing the fission chamber response in terms of fission rate. This way, the detector calibration coefficient is independent from the neutron spectrum and can be determined prior to the experiment. The fissile deposit response to the neutron spectrum can then be assessed independently by other means (experimental or numerical). In this paper, the response of CEA made miniature fission chambers in Campbelling mode is studied. We use a theoretical model of the signal to calculate the calibration coefficient. Input parameters of the model come from statistical distribution of individual pulses. Supporting measurements have been made in the CEA Cadarache zero power reactor MINERVE and results are compared to an empirical Campbelling mode calibration. The tested fission chamber calibration coefficient is about 2 × 10^{-26} A^2 Hz^{-1} c^{-1}. Both numerical and empirical methods give consistent results, however a deviation of about 15 % was observed.

I. INTRODUCTION

I. INTRODUCTION

T is generally accepted that fission chambers can be used in three operation modes. At low neutron fluxes, the fission rate in the fissile deposit is low enough and fission products induced pulses are scarce (i.e. the average delay between two pulses is much larger than the pulse duration). They can be counted so as to obtain an event rate closely related to the detector fission rate: this is known as the “pulse mode”. With the neutron flux increasing, pulses inside the chamber overlap and cannot be individually processed anymore. An indirect parameter related to the fission rate must be measured, namely the average current delivered by the detector in the “current mode” or the variance of the current in the so-called “Campbelling mode”. Indeed, if the process underlying the detection of neutrons is Poissonian, Campbell has demonstrated that both the current mean and variance are strictly proportional to the event rate [1].

The Campbelling mode is of great interest as it drastically diminishes the disturbance of gamma rays on fission chamber neutron signal [2][3].

Campbell theorems have been generalized to higher order statistics [4]. Recently, a new approach has been developed to model fission chamber signal [5]. It gives n-th order cumulants and spectra formula by using a model based on a random vector describing the current pulses (pulse shapes, deposited charge, etc.)

Our purpose here is to apply the same fission chamber modeling approach to the detector calibration in Campbelling mode (i.e. for the second order). This work has been done in the framework of the research activities in fission chamber modeling conducted at CEA Cadarache [6].

The fission chamber calibration problem is described in section II. General formulas adapted for our measurement setup are given in section III. In section IV the experimental setup we used to validate our method is presented. We chose to irradiate a CEA-made miniature fission chamber in the zero power pool reactor MINERVE (Cadarache, France). Major experimental results are then presented and discussed in section V.

II. FISSION CHAMBER CALIBRATION

The fission rate $R$ of a detector fissile deposit composed of $N$ fissile atoms can be related to the neutron flux $\Phi$ and to the overall fission cross section $\overline{\sigma}$ is expressed as:

$$ R / N = \overline{\sigma} \cdot \Phi $$

(1)

By calculating the fission cross section, one can derive the on-line neutron flux. Inversely, by knowing the neutron flux, one can have access to an estimate of the fission cross section.

In the case of a detector with a thick fissile deposit, it is necessary to introduce an additional coefficient $k_o$ to take into account the signal loss due to the self-shielding (i.e. the neutron flux level depression mostly due to neutron absorption) and auto-absorption (accounted for by the stopping of fission products inside the deposit). Consequently, under the assumption that the “lost” fission products are not statistically different from the others, an “active fissile mass” composed of $N_a$ fissile atoms can be defined as: $N_a = k_o \times N$.

So, the “active fission rate” can be defined as $R_a = N_a \cdot \overline{\sigma} \cdot \Phi$. 
$R_a$ is obviously the only quantity directly accessible to the measurement. The determination of the auto-absorption factor is not our purpose here, so in the following it will be assumed that the $k_o$ is equal to 1 (i.e. $R = R_o$).

Fig. 1 exhibits a general diagram describing fission chamber calibration shall now be presented. The relation between $R$ and $\Phi$ allows us to use a coefficient $K_\Phi$ that depends solely on the neutron properties of the fissile deposit. A second coefficient $K_d$ is used to link the fission rate to the signal $S_d$ generated inside the detector. $K_d$ depends solely on the chamber response (gas mixture, pressure and geometry). Last, $K_r$ links the detector signal $S_d$ to the measurement $S_r$ and is related to the electronic system.

III. CALIBRATION METHOD IN CAMPBELLING MODE

In Campbelling mode, $S_d$ is the average amplitude of the power spectrum density of the output current. $S_d$ is expressed in $A^2/Hz$ and so $K_d$ is expressed in $A^2/Hz/(c/s)$. $K_d$ can be understood as the response of fission chamber to an average fission product emitted by the fissile deposit.

After the second Campbell theorem it is known that coefficient $K_d$ is related to the second order statistics of individual pulses occurring in the detector. We also know how to link the signal spectrum to the physical parameters of the detector [5].

As a result, one can show that the detector calibration factor is expressed as:

$$K_d = \left(\frac{\overline{Q}^2 + \sigma_Q^2}{\Delta T} \right) \cdot \frac{\Delta T}{F_2 - F_1} \cdot \int F_T \left[ \overline{h}^2 \right]^2 dF,$$

where $FT$ is the Fourier transform operator, $\overline{Q}$ (in C) and $\sigma_Q^2$ (in C²) are the first two moments of the collected charge statistics, $\overline{h}$ (expressed in $s^1$) is the average pulse at the output of the detector, $\Delta T$ (in s) is the average pulse width and $F_2 - F_1$ is the measurement frequency range (in Hz).

This calibration method is based on acquiring individual pulses at the output of a fast broadband amplifier. Voltage signal has to be directly proportional to the current delivered by the detector. The signal to noise ratio has to be high enough so that the pulse discrimination does not greatly modify the statistical distributions of relevant parameters. Terms of (2) are calculated and reconstructed afterwards by straightforward numerical processing.

IV. EXPERIMENTAL SETUP

MINERVE is a pool type ZPR operated by CEA Cadarache. The facility is dedicated to experimental programmes in support of the French nuclear industry and to improve neutron cross sections databases. Its maximum power is 80 W. Two irradiation channels are available to test fission chambers in a nearly thermal neutron flux (about $10^8$ n/cm²/s at maximum power).

Our test detector is a miniature cylindrical CF4 type fission chamber manufactured at Cadarache Fission Chamber Workshop [7]. This detector (FC 2247) houses a 250 μg deposit of enriched uranium (98.5% U-235). An estimation of the deposit thickness is 0.6 μm. The detector outer diameter is 4 mm and the electrode gap is 0.5 mm. The fill gas is pure argon at 12 bars.

Measurements in Campbelling mode were acquired using a new acquisition system called the Fast Neutron Detector System (FNDS). This system has been developed and qualified in the framework of the Instrumentation Joint Laboratory that regroups CEA and SCKCEN [8].

The FNDS acquisition system is sketched on Fig. 2. Its front end is a fast broadband current amplifier (gain of about 32500). The variance measurement is taken on a frequency range spanning from 20 kHz to 300 kHz (analog pass-band filter, 8th order) and the acquisition frequency is 1 MHz. The electronics gain has been calibrated using synthesized signals: $K_r$ is about $10^{15}$ Ω².Hz.

V. MAJOR RESULTS AND DISCUSSION

A. Calibration in pulse mode

Our test detector signal was compared to the one of a calibrated fission chamber (FC 2232, same geometry, 25 μg U-235). The measurement was done in the irradiation channel n°2 at a power of 10 W. Our calibrated detector gave us a fission rate of $R_{at}$ = 27.9 c/s/μg. The measurement is done using a standard Pulse Height Analysis channel (using Canberra spectroscopy electronic modules).
FC 2247 PHA spectrum gives us a counting rate depending on the discrimination threshold (expressed as a fraction of a reference channel C, see Fig. 3). We define the equivalent uranium mass as the mass that corresponds to a fission rate equal to the counting rate.

At low threshold, the noise level introduces a bias in the estimation of the counting rate (as we can see on Fig. 3, the counts increase below 0.1C). To circumvent that issue, we used an extrapolation of the equivalent mass down to a zero threshold. The obtained active uranium mass for FC 2247 is 219 μg. There is a 12 % deviation between this mass and the total mass coated on the electrode (around 250 μg). This deviation can be explained by the auto-absorption effect [9].

By multiplying the active mass by the fission rate per atom, we can obtain the total event rate inside the detector. Based on this measurement, we will subsequently use an empirical factor to convert a counting rate obtained for a specific threshold into the total event rate. This factor is equal to 1.1 for a typical threshold of 0.3C.

![Fig. 3. FC 2247 PHA spectrum at 10W. The reference channel C is determined based on the spectrum maximum. An extrapolation of the spectrum below 0.1C allows us to estimate the active mass of the fissile deposit.](image)

**B. Detector linearity with reactor power**

One of the main goals of the measurement campaign was to test the linearity of the detector by measuring the Campbelling mode signal at various reactor power levels. We tested 5 power levels from 1 W to 80 W. The detector was installed in the irradiation channel n°2 at core mid-plane and polarized at 300 V.

At high power (80 W) a broadband spectrum of the signal at the FNDS preamplifier output was acquired on-line using an oscilloscope (LeCroy WaveRunner, 500 MHz bandwidth and maximum sampling 5 GS/s). FNDS signal spectrum was also calculated afterwards using samples of acquired signals. Both spectra are compared in Fig. 4.

The plot of the FNDS spectrum clearly shows the effect of the pass-band filter that eliminates the ionic signal part (below 20 kHz) is clearly observed. The frequency domain is nearly flat, which is in favor of the measurement steadiness.

FNDS variance measurements (in V²) were converted into power spectrum densities by using electronics calibration factor $K_e = 10^{15} \Omega^2 \text{Hz}$. At each power level, a counting rate measurement was performed and converted into total event rates by using the pulse calibration factor.

Fig. 5 shows that the detector linearity is very good over nearly two decades. The first measurement point is close to the FNDS noise background (about $10^{-7} \text{V}^2$) and it was necessary to subtract the noise from the signal.

The linear fit gives a empirical estimation of the calibration coefficient of $1.8 \times 10^{-26} \text{A}^2/\text{Hz}/(\text{c/s})$. The uncertainty of this result is difficult to assess since it depends mostly on the pulse calibration factor. We estimate that it is around 10 % (68 % confidence interval).

![Fig. 4. FC 2247 spectra acquired with a broadband oscilloscope and with FNDS (frequency range 20 kHz to 300 kHz).](image)

![Fig. 5. Campbelling mode signal acquired by FNDS versus the total event rate in the FC 2247. The linear fit slope gives us an estimation of the Campbelling mode calibration factor $K_d$.](image)

**C. Pulses measurements**

Detector signals were acquired at FNDS preamplifier output in order to access statistical properties of delivered pulses (collected charge, pulse width, pulse shapes). Our objective here is to estimate every parameters needed to apply (2).

Individual pulses were acquired at low power (10 W) using the oscilloscope. The event rate in the detector is lower than $10^4$ pulses per second. Fig. 6 shows the detector average pulse as well as the pulse shape standard deviation (upper plot). The charge spectrum was calculated offline (lower plot). It is found to be is very consistent with the one obtained by a standard PHA measurement.

Main calculated parameters of the average pulse are summarized in Table I. As it can be seen, the average charge
coming from the electronic component of the pulse is not
equal to the charge collected from the ionic part. That comes
from the fact that the charges are not uniformly created in the
electrode gap. On the contrary, charges are mostly created
close to the fissile deposit, so the electrons’ path in the gas is
on average smaller than the ions path.

The sum of the electronic and ionic charges gives us the
total charge $Q$ deposited by an average fission product in the
detector. This quantity is often expressed in terms of number
of electrons. In our case, we have on average $1.4 \times 10^6$ electrons
by fission product. Charge standard deviation
$\sigma_Q$ was found to be 33 \% of the average charge.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|}
\hline
Parameter & Electronic component & Ionic component \\
\hline
Width & 150 ns & 40 $\mu$s \\
Amplitude & 1.4 $\mu$A & 7.2 nA \\
Charge & 91 fC & 132 fC \\
\hline
\end{tabular}
\caption{FC 2247 pulse parameters}
\end{table}

Using the parameters in Table I and by numerically
computing the Fourier transform of the pulse shape, we were
able to calculate the calibration coefficient solely based on
pulse measurements.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{pulse_shape}
\caption{Average pulse acquired at FNDS preamplifier output (upper plot). Charge spectrum (lower plot) based on individual pulses analysis (blue) and measured using a standard PHA channel (red).}
\end{figure}

Our calculation gave us a $K_d$ equal to $2.05 \times 10^{-26}$ A$^2$/Hz/(c/s).
That value is consistent with the empirical value of $1.8 \times 10^{-26}$
A$^2$/Hz/(c/s). The deviation of 14 \% between the two values
can most likely be attributed to the imperfections of our
estimation of the detector total counting rate. Another source

\section{VI. Conclusion}
In this paper a method is detailed to calibrate fission
chambers in Campbelling mode. It is based on characterizing
the detector pulses and calculating the detector response using
a detailed expression of Campbell’s second theorem.

Results acquired at the MINERVE reactor using a CEA
made miniature fission chamber with 250 $\mu$g uranium deposit
demonstrated the feasibility of the method. The obtained
calibration coefficient is $2.05 \times 10^{-26}$ A$^2$/Hz. A 14 \% deviation
between this value and the reference one based on a
calibration of the detector in pulse mode was observed.

In a subsequent work, we plan to further test the robustness
of the method and apply it to other miniature fission chambers
with various technological parameters (gas mixture, pressure
and fissile deposit).

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