BISON TRISO Training Material

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March 2020



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TRISO in BISON

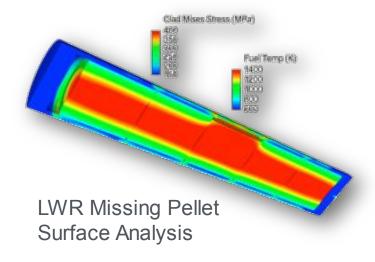
Computational Mechanics and Materials Idaho National Laboratory

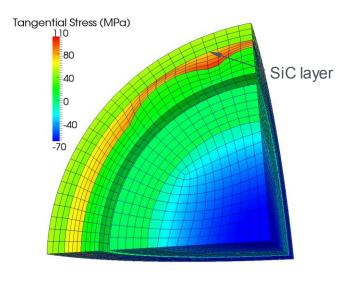
History of BISON

NEAMS/CASL Fuels Programs

Historical Overview

- Overarching objective to deliver an integrated set of predictive computational tools for nuclear fuel performance analysis and design
- A multiscale approach has been adopted in which engineering-scale simulations are informed by mesoscale simulations of microstructure evolution, which are enabled by parameters obtained from atomistic simulations
- Primary products are BISON for engineering-scale analysis and Marmot for mesoscale analysis, both built upon the MOOSE computational framework





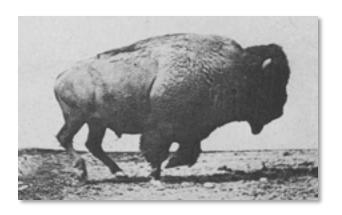
Defective TRISO Particle

Bison: What is it?



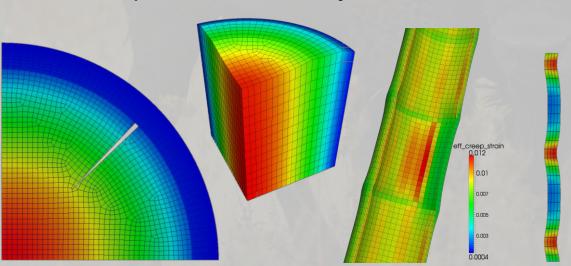


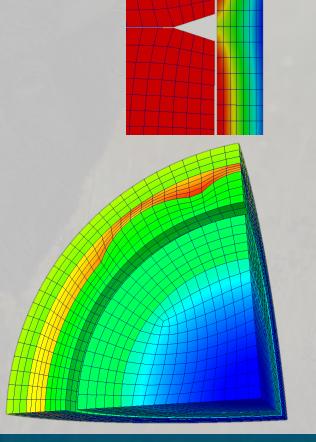
- Bison once numbered in the tens of millions and ranged over much of North America.
- Bison can weigh 1000+ kg and stand
 1.8+ m high at the shoulder.
- Bison can jump 1.8 m vertically.
- Bison can run 60+ km/h.



BISON: What is it?

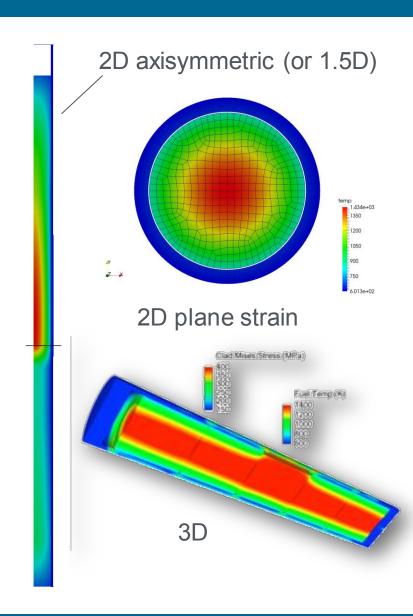
- A finite element, thermo-mechanics code with material models and other customizations to analyze nuclear fuel
 - Accepts user-defined meshes/geometries
 - 1D, 2D, or 3D
 - Runs on one processor or many
 - Analyzes a variety of fuel types
 - Couples to other analysis codes





BISON Fuel Performance Code

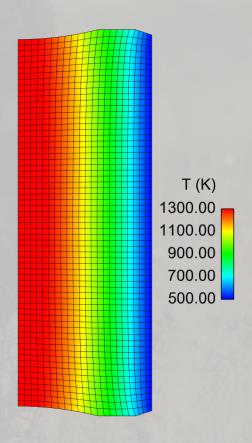
- Finite element-based engineering scale fuel performance code
- Solves the fully-coupled thermomechanics and species diffusion equations in 1D, 1.5D,
 2D axisymmetric or plane-strain, or full 3D
- Used for LWR, ATF, TRISO, and metallic fuels
- Applicable to both steady and transient operations and includes LOCA and RIA capability for LWR fuel
- Readily coupled to lower length scale material models
- Designed for efficient use on parallel computers
- Development follows NQA-1 process



BISON Requirements and Limitations

BISON requires:

- An input file that describes thermal and mechanical material models, boundary conditions, initial conditions, power history
- A mesh provided either directly in the input file or through a separate mesh file
- BISON cannot currently model:
 - Very high strain rate analyses (e.g., car crashes)
 - Structural elements (membranes, shells, beams)
 - Melting or flowing material
- BISON is not:
 - A thermal-hydraulics or CFD code
 - A neutronics code





BISON Governing Equations

Energy conservation (transient heat conduction with fission source)

$$\rho \, c_p \, \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + E_f \dot{F} \qquad \qquad \text{Fission density rate = f(x, t)}$$

Species conservation (transient oxygen or fission product diffusion with radioactive

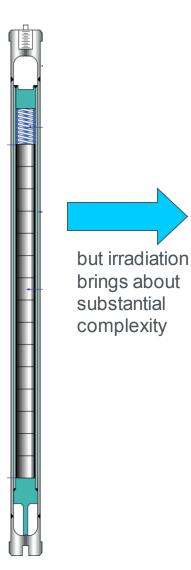
decay) Fickian diffusion
$$\frac{\partial C}{\partial t} = \nabla \cdot D \left(\nabla C - \frac{CQ}{FRT^2} \nabla T \right) - \lambda C + S$$
 Radioactive decay

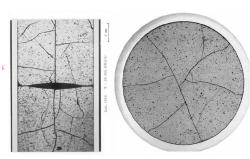
Momentum conservation (Cauchy's equation of equilibrium)

$$\nabla \cdot \mathbf{T} + \rho \mathbf{f} = 0$$

Fuel Behavior During Irradiation

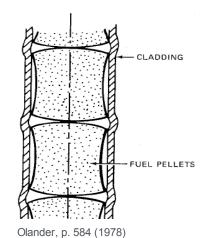
At beginning of life, a fuel element is quite simple . . .



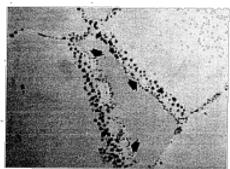


Michel et al, Eng Frac Mech, 75, 3581 (2008)

Fuel Fracture

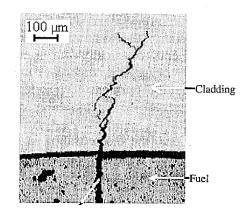


Multidimensional contact and deformation



Olander, p. 323 (1978)

Fission gas



Bentejac et al, PCI Seminar (2004)

Stress Corrosion Cracking Cladding Failure

Fuel Behavior Modeling: Coupled Multiphysics and Multiscale

Multiphysics

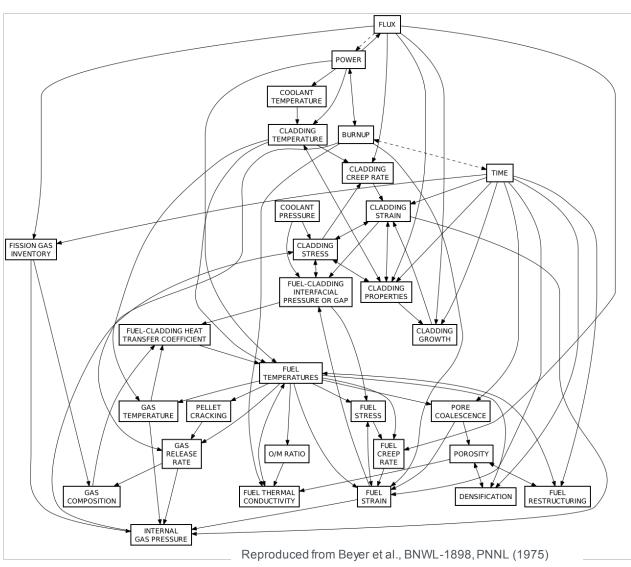
- > Fully-coupled nonlinear thermomechanics
- > Mass transport
- > Chemistry
- > Neutronics
- > Thermal-hydraulics

Multi-space scale

- Important physics operate at level of microstructure
- Need real predictions at engineering scale

Multi-time scale

- Long, steady operation
- > Short power ramps
- > Rapid transients



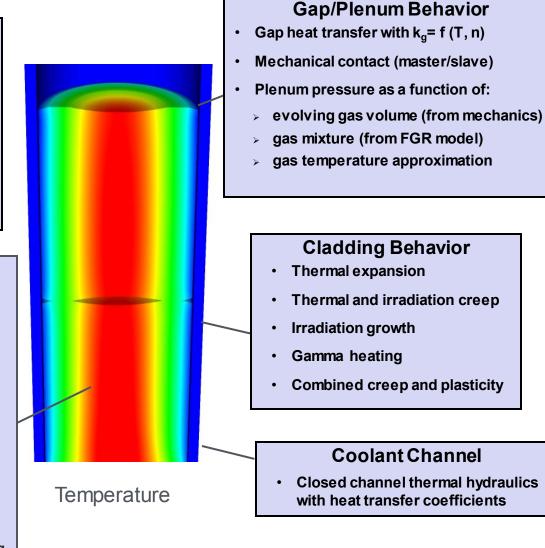
BISON Application: LWR Fuel

General Capabilities

- Finite element based 1D spherical, 2D-RZ and 3D fully-coupled thermo-mechanics with species diffusion
- Linear or quadratic elements with large deformation mechanics
- · Steady and transient operation
- Massively parallel computation
- Meso-scale informed material models

Oxide Fuel Behavior

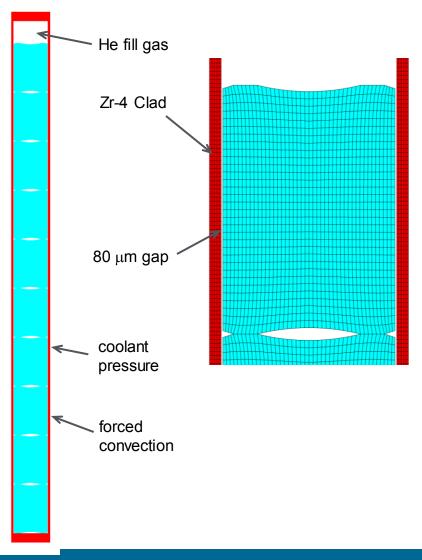
- Temperature/burnup dependent conductivity
- Heat generation with radial and axial profiles
- Thermal expansion
- Solid and gaseous fission product swelling
- Densification
- Thermal and irradiation creep
- Fracture via relocation or smeared cracking
- Fission gas release (two stage physics)
 - > transient (ramp) release
 - grain growth and grain boundary sweeping
 - athermal release

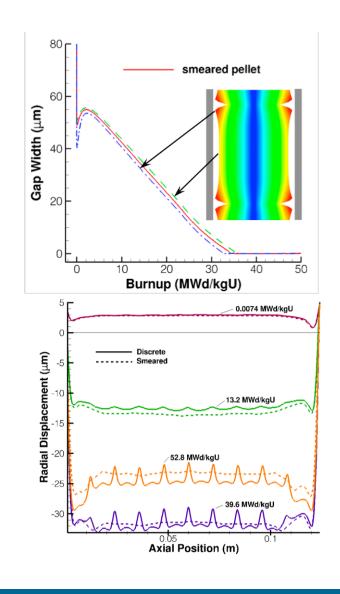


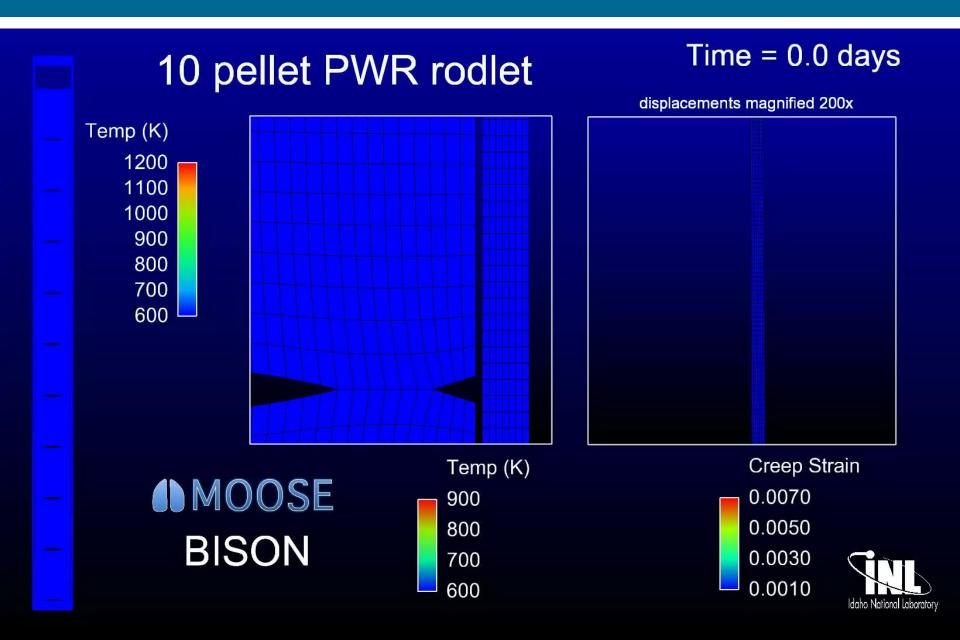
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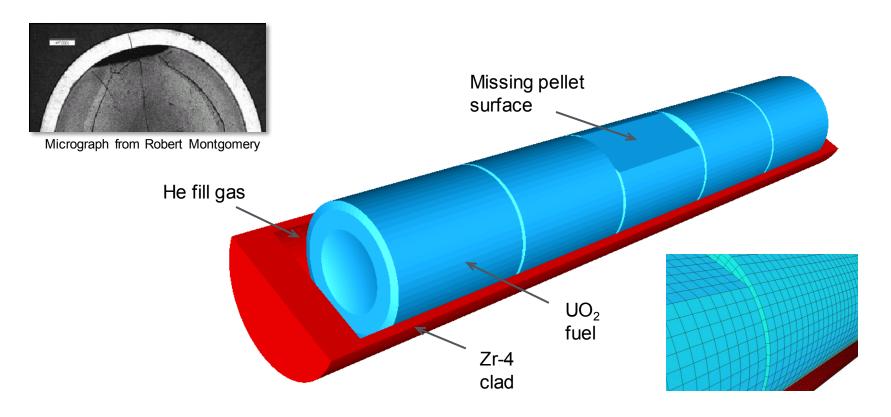
Discrete Pellet LWR Rodlet (2D-RZ multiphysics)







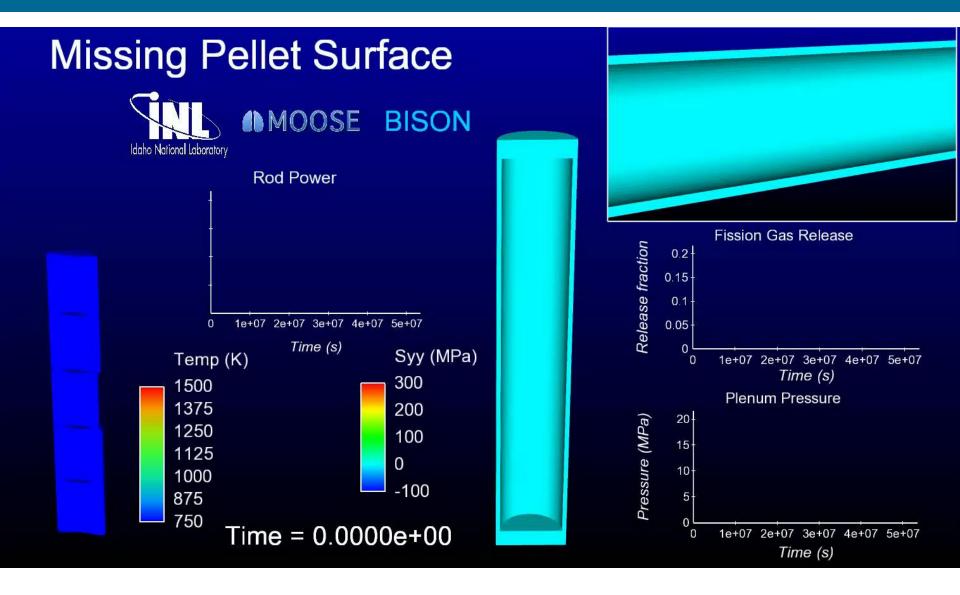
PCMI - Missing Pellet Surface Analysis



- High resolution 3D calculation (250,000 elements, 1.1x10⁶ dof) run on 120 processors
- Simulation from fresh fuel state with a typical power history, followed by a late-life power ramp

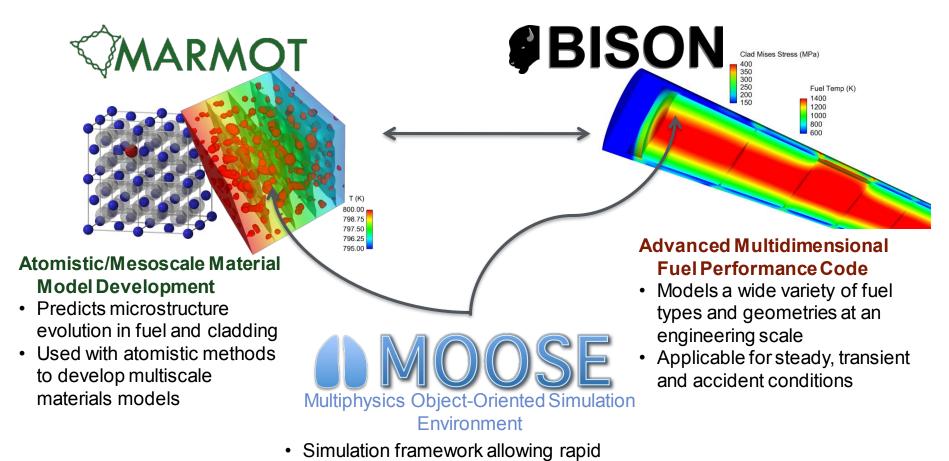
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Animation – Missing Pellet Surface with Power Ramp



MOOSE-BISON-Marmot (MBM)

 The MOOSE-BISON-Marmot (MBM) codes provide an advanced multidimensional, multiphysics, multiscale fuel performance capability



development of FEM-based applications

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Nuclear Energy Modeling and Simulation Program

Fuels Technology Area

- New program (FY20+) combines Fuels scope from both NEAMS and CASL
 - Advanced Reactors (Metallic, TRISO, UC/UN)
 - Light Water Reactors (ATF, Increased Enrichment and Extended Burnup, Accident Analysis)
 - Code framework advancements (Robustness, Speed, Ease-of-Use, Documentation, Software Quality)
- Early stage R&D performed must be relevant to industry and coordinated with the NRC
- FY20 Work Packages: Managers
 - Engineering Scale Advanced Reactor Fuel Performance: Steve Novascone
 - Engineering Scale LWR Fuel Performance: Giovanni Pastore
 - Advanced Numerical Model Development and Usability Improvements: Daniel Schwen
 - Lower Length Scale Model Development: Larry Aageson
 - Lower Length Scale Model Development LANL: David Andersson
 - Metallic Fuel Development and Validation ANL: Latif Yacout
 - Thermochemistry Model Development ORNL: Srdjan Simunovic

Questions?



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TRISO in BISON

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MOOSE

MOOSE

- MOOSE website
 - <u>https://mooseframework.org/</u>
- Input file syntax definitions and class documentation
 - https://mooseframework.org/syntax/index.html
- MOOSE physics modules
 - https://mooseframework.org/modules/index.html
- MOOSE workshop
 - https://mooseframework.org/workshop/#/

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Questions?



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TRISO in BISON

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TRISO in BISON circa 2013 and Today

TRISO in BISON circa 2013

- Rich Williamson started BISON with INL LDRD funds over ten years ago.
- In 2012, the first major BISON paper was published.
 - http://dx.doi.org/10.1016/j.jnucmat.2012.01.012
 - Paper focused on LWR fuel but also had a TRISO example
 - TRISO analysis featured heat conduction and species diffusion
- At about that time, the BISON team decided to add a baseline TRISO capability, including thermal, mass diffusion, and mechanical models.



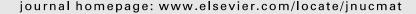
BISON TRISO Paper, JNM 2013

Journal of Nuclear Materials 443 (2013) 531–543



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Journal of Nuclear Materials





Multidimensional multiphysics simulation of TRISO particle fuel



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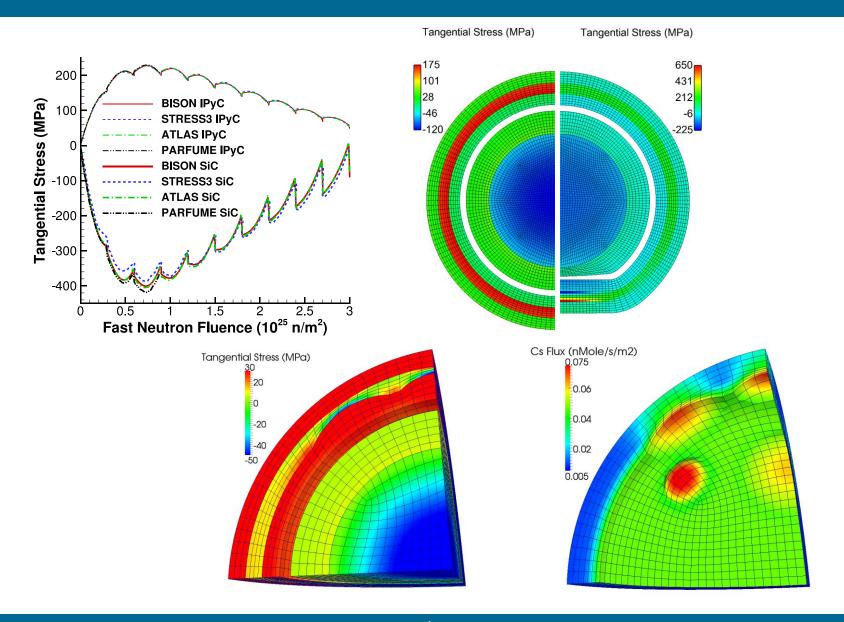
ABSTRACT

Multidimensional multiphysics analysis of TRISO-coated particle fuel using the BISON finite element nuclear fuels code is described. The governing equations and material models applicable to particle fuel and implemented in BISON are outlined. Code verification based on a recent IAEA benchmarking exercise is described, and excellent comparisons are reported. Multiple TRISO-coated particles of increasing geometric complexity are considered. The code's ability to use the same algorithms and models to solve problems of varying dimensionality from 1D through 3D is demonstrated. The code provides rapid solutions of 1D spherically symmetric and 2D axially symmetric models, and its scalable parallel processing capability allows for solutions of large, complex 3D models. Additionally, the flexibility to easily include new physical and material models and straightforward ability to couple to lower length scale simulations makes BISON a powerful tool for simulation of coated-particle fuel. Future code development activities and potential applications are identified.

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http://dx.doi.org/10.1016/j.jnucmat.2013.07.070

BISON TRISO Paper, JNM 2013



TRISO Stagnation

- After the 2013 paper, we talked with potential stakeholders about our capability.
- But, very little interest.
- No interest → no funding → no development.
- Added an internal 1D TRISO mesh generation capability in 2018.
- Things started to pick up in FY19.



Recent Interest in TRISO in BISON







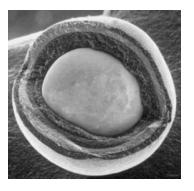




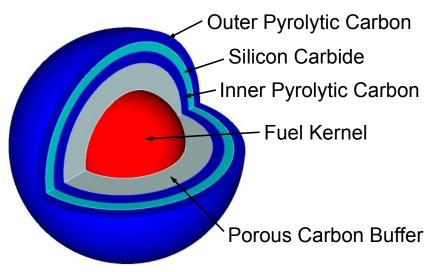


Current TRISO Development

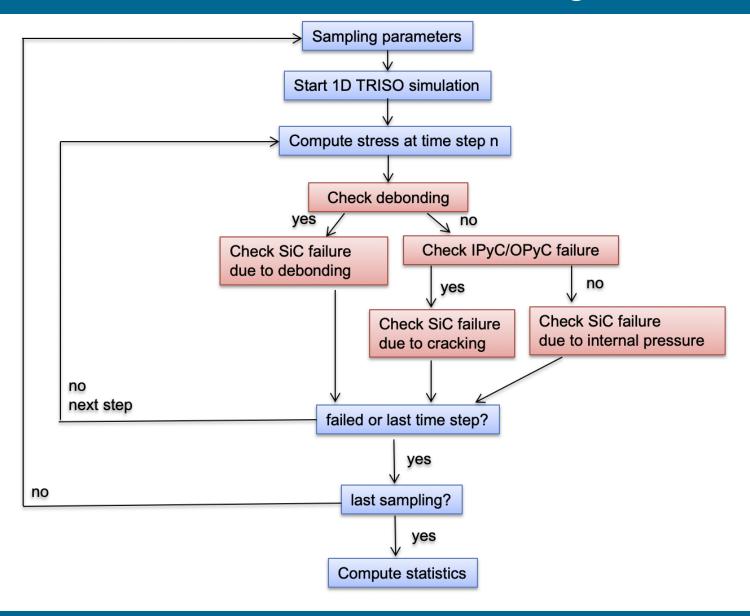
- Adding more complete set of models from PARFUME
 - Elastic properties
 - Thermal properties
 - Mass diffusion properties
 - Kernel
 - Swelling
 - Fission gas release
 - Buffer
 - Creep
 - Irradiation strain



- PyC
 - Creep
 - Irradiation strain
- SiC
 - Palladium penetration
- Matrix



Current TRISO Development Continued: Monte Carlo Scheme for Predicting Failure



Questions?









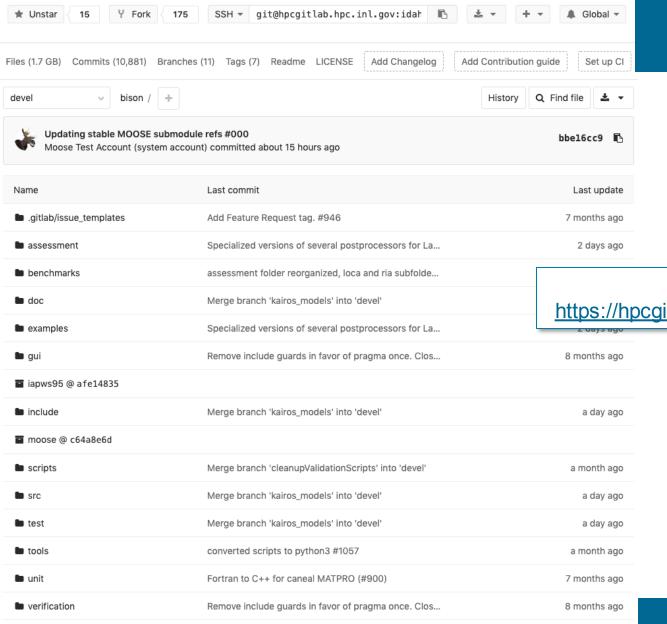
TRISO in BISON

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Organization of BISON Code, Tests, and Examples

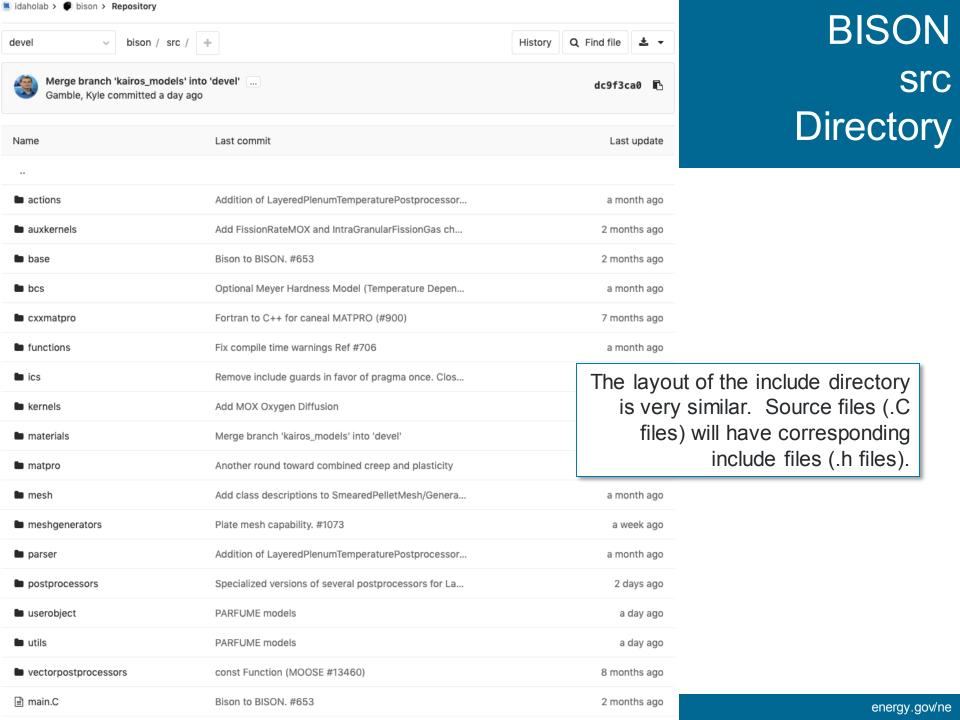


Nuclear Fuel Performance Code



BISON Repository Layout

This is the view from https://hpcgitlab.inl.gov/idaholab/bison



BISON test/tests Directory

| /Users/halejd/gitProjects/bisor |
|---------------------------------|
| inl604289 devel> ls test/tests |
| 2d_arrhenius/ |
| ADMetallicFuelWastage/ |
| Al203/ |
| GrainRadiusPorosity_test/ |
| GraphiteMatrixElasticityTensor/ |
| GraphiteMatrixSpecificHeat/ |
| GraphiteMatrixThermalConductivi |
| MetallicFuelWastage/ |
| OxideEnergyDeposition/ |
| ThermalFuel_error_messages/ |
| VSwellingU3Si2/ |
| ad_arrhenius_material_property/ |
| ad_ht9_thermal/ |
| ad_upuzr_burnup/ |
| ad_upuzr_fast_neutron_flux/ |
| ad_upuzr_fission_gas_release/ |
| ad_upuzr_fission_rate/ |
| ad_upuzr_thermal/ |
| anisotropic_swelling/ |
| arrhenius_diffusion_coef/ |
| arrhenius_material_property/ |
| average_axial_position/ |
| average_burnup/ |
| axial_relocation/ |
| burnup_action/ |
| carbon_monoxide_production/ |
| check_error/ |
| circular_cross_section_mesh/ |
| constitutive_heat_conduction/ |
| convective_heat_transfer/ |
| coolant_channel_model/ |
| creep_HT9/ |
| creep_S1C/ |
| creep_U10Mo/ |
| creep_mox/ |
| creep_uo2/ |
| creep_upuzr/ |
| cumulative_damage_index/ |
| decay_heating/ |
| diffusion_limited_reaction/ |
| dislocation_density/ |
| |

```
dryCask/
    effective burnup aux/
    element integral power/
    example problem test/
    failure cladding zr/
    failurecladHT9/
ity/ fast neutron_flux/
    fcci_ht9/
    fecral/
    fecral oxidation/
    fgr_fraction/
    fgr_percent/
     fgr_upuzr/
    fill_gas_thermal_conductivity/
    fission gas 1d/
    fission gas behavior sifgrs/
    fission gas behavior u3si2/
    fission gas release formas/
    fission_rate_LWR/
    fission_rate_MOX/
    fission_rate_axial/
    fission_rate_from_power_density/
    fission_rate_heat_source/
    fission to thermal power/
    fuelrodlinevaluesampler/
    gamma heating/
    gap heat transfer/
    gap_heat_transfer_fission/
    gap heat transfer htonly/
    gap heat transfer mixedgas/
    gap_heat_transfer_radiation/
    gap_jump_distance/
    gap_perfect_transfer/
    generic material failure/
    grain radius aux/
    hotpressing uo2/
    hydride/
    hydrogen/
    ifba he production/
    increment limited time step/
    irradiation growth/
```

```
irradiation growth Zr4/
layered2D/
layered 1D/
mamox/
mechHT9/
mechTests/
mechZrv/
mechanical uo2/
meso thrond test/
mox_oxygen_to_metal_ratio/
mox_pore_velocity/
oxidation cladding/
oxygen aux/
oxygen transport/
partial sum heat flux/
percolation/
performance outputs action/
phase transition zircaloy/
phase upuzr/
plate mesh/
plenum pressure/
plenum_temp/
power peaking function/
radial avg fuel enthalpy/
radial crack counter/
radial power factor/
radioactive decay/
radius aux/
relocation UO2/
relocation_recovery_U02/
side_ave_incr_tensor_component/
side_int_var_incr_postprocess/
side_integral_mass_flux/
smeared pellet mesh/
smeared_pellet_mesh_generator/
solid_mechanics_deprecated/
stan neumann/
standard lwr outputs action/
submodel end bc/
swelling/
temperature jump_distance/
```

```
tensor_mechanics/
thermalCompositeSiC/
thermalD9/
thermalFastMOX/
thermalFeCrAl/
thermalFuel HaldenMOX/
thermalFuel HaldenUO2/
thermalFuel NFIR/
thermalFuel NFImod/
thermalHT9/
thermalMAMOX/
thermalMOX/
thermalMonolithicSiC/
thermalNa/
thermalSilicideFuel/
thermalTests/
thermalU02/
```

BISON has about 1800 regression tests.

```
thermal_expansion_zry/
thermal irradiation creep/
thermal_irradiation_creep_plas/
thermirrad creep zr42/
thermo mech oxygen/
triso/
triso failure/
un_swelling/
upuzr burnup/
upuzr dictra/
upuzr_diffusivity/
upuzr fast neutron flux/
upuzr_fission_rate/
upuzr_phase_lookup/
vswelling upuzr/
zirconium diffusion/
zrdiffusivity_upuzr/
zrh_formation/
zry plasticity/
```

BISON examples Directory

```
/Users/haleid/gitProjects/bison
inl612500|devel> ll examples/
1.5D restart/
                        2D plane strain rod/
                                                accident_tolerant_fuel/ metal_fuel/
                                                                                                 non-cylindrical fuel/
                                                                                                                          restart/
                                                axial relocation/
1.5D rodlet 10pellets/ 3D rodlet 3pellets/
                                                                         mox fuel/
                                                                                                 percolation/
                                                                                                                          spent fuel/
2D-RZ rodlet 10pellets/ TRISO/
                                                fast mox sifgrs/
                                                                         multiapp/
                                                                                                 pore migration/
                                                                                                                          temperature tables/
/Users/halejd/gitProjects/bison
inl612500|devel> ll examples/TRISO/
total 0
drwxr-xr-x
                                              192B Feb 21 14:47 ./
             6 haleid INEL-NT\Domain Users
drwxr-xr-x 20 haleid INEL-NT\Domain Users
                                              640B Feb 21 14:47 ../
drwxr-xr-x
            9 halejd INEL-NT\Domain Users
                                              288B Feb 21 14:47 accident_simulation/
            4 haleid INEL-NT\Domain Users
                                              128B Feb 21 14:47 full particle/
drwxr-xr-x
            4 haleid INEL-NT\Domain Users
                                              128B Feb 21 14:47 one layer/
drwxr-xr-x
                                              128B Feb 21 14:47 two_layers/
drwxr-xr-x
            4 haleid INEL-NT\Domain Users
/Users/halejd/gitProjects/bison
inl612500|devel> ls examples
1.5D restart/
                        2D_plane_strain_rod/
                                                accident tolerant fuel/ metal fuel/
                                                                                                 non-cylindrical fuel/
                                                                                                                          restart/
1.5D rodlet 10pellets/ 3D rodlet 3pellets/
                                                axial relocation/
                                                                         mox fuel/
                                                                                                 percolation/
                                                                                                                          spent fuel/
2D-RZ_rodlet_10pellets/ TRISO/
                                                fast mox sifgrs/
                                                                         multiapp/
                                                                                                 pore_migration/
                                                                                                                          temperature_tables/
/Users/halejd/gitProjects/bison
inl612500|devel> ls examples/TRISO/
accident simulation/ full particle/
                                          one layer/
                                                                two layers/
/Users/halejd/gitProjects/bison
inl612500|devel> ls examples/TRISO/full particle/
1D/ 2D/
/Users/halejd/gitProjects/bison
inl612500|devel> ls examples/TRISO/full particle/1D
examples
                    full_particle_1D.i gold/
                                                             tests
```

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```
DO NOT MODIFY THIS HEADER
       Under Contract No. DE-AC07-05ID14517
       See COPYRIGHT for full restrictions
#include "UCOVolumetricSwellingEigenstrain.h"
registerMooseObject("BisonApp", UCOVolumetricSwellingEigenstrain);
template <>
InputParameters
validParams<UCOVolumetricSwellingEigenstrain>()
  InputParameters params = validParams<ComputeEigenstrainBase>();
 params.addClassDescription("Fission-induced swelling (percent per percent FIMA) for UCO");
 params.addParam<Real>("swelling_scale_factor", 1.0, "Multiplier for UCO swelling");
  return params;
    const InputParameters & parameters)
  : ComputeEigenstrainBase(parameters),
   swelling scale factor(getParam<Real>("swelling scale factor")),
   _burnup(getMaterialProperty<Real>("burnup")),
   _swelling(declareProperty<Real>("swelling"))
UCOVolumetricSwellingEigenstrain::initQpStatefulProperties()
  _swelling[_qp] = 0;
  ComputeEigenstrainBase::initQpStatefulProperties();
UCOVolumetricSwellingEigenstrain::computeOpEigenstrain()
 Real volumetric_swelling_strain = _swelling_scale_factor * 0.8 * _burnup[_qp];
 Real strain component = computeVolumetricStrainComponent(volumetric swelling strain);
  _swelling[_qp] = volumetric_swelling_strain;
  _eigenstrain[ qp].zero();
  _eigenstrain[_qp].addIa(strain_component);
```

Example **BISON** Source File

src/materials/tensor mechanics/UCOVolumetricSwellingEigenstrain.C

Example BISON Test

```
/Users/halejd/gitProjects/bison
inl604289|devel> ls test/tests/triso/UCOVolumetricSwellingEigenstrain/
UCOVolumetricSwellingEigenstrain.i gold/
UCOVolumetricSwellingEigenstrain_out.csv tests
```

```
/Users/halejd/gitProjects/bison
inl604289|devel> cat test/tests/triso/UCOVolumetricSwellingEigenstrain/tests
[Tests]
  [./UCOVolumetricSwellingEigenstrain]
    type = 'CSVDiff'
    input = 'UCOVolumetricSwellingEigenstrain.i'
    csvdiff = 'UCOVolumetricSwellingEigenstrain_out.csv'
    requirement = "BISON shall calculate volumetric swelling of UCO."
    design = 'UCOVolumetricSwellingEigenstrain.md'
    issues = '#1074'
[../]
[]
```

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Example BISON Test Continued

```
UCO fission-induced swelling
 The geometry is a unit cube made of UCO subject to burnup-induced swelling.
# The swelling is simply 0.8 * burnup. Burnup is ramped from 0 to 0.125.
# Thus, swelling increases to 0.1. The final volume is 1.1.
[GlobalParams]
 # Set initial fuel density, other global parameters
 displacements = 'disp x disp y disp z'
 volumetric locking correction = true
 order = FIRST
 family = LAGRANGE
\Pi
[Mesh]
  [mesh]
   type = GeneratedMeshGenerator
   dim = 3
   xmax = 1.0
   ymax = 1.0
   zmax = 1.0
  []
[Problem]
  coord type = XYZ
```

View remainder of input file in editor.

Example BISON Example

```
/Users/halejd/gitProjects/bison
inl612500|devel> ls examples/TRISO/full_particle/1D
examples full_particle_1D.i gold/ tests

/Users/halejd/gitProjects/bison
inl612500|devel> cat examples/TRISO/full_particle/1D/tests
[Tests]
  [./full_particle]
    type = RunApp
    input = 'full_particle_1D.i'
    check_input = True
    method = opt
  [../]
[]
```

Example BISON Example Continued

```
[GlobalParams]
 density = 10810.0
 order = SECOND
 family = LAGRANGE
 displacements = 'disp_x'
[Mesh]
 type = TRIS01DMesh
 elem_{type} = EDGE3
 coordinates = '0 2.485e-4 3.425e-4 3.425e-4 3.835e-4 4.195e-4 4.595e-4'
 mesh density = '6 6 0 6 8 6'
 block_names = 'fuel buffer IPyC SiC OPyC'
[Problem] SC
 coord_type = RSPHERICAL
[Variables]
 [./temperature]
   initial condition = 1346.0
[AuxVariables]
 [./fluence]
 [./fast neutron flux]
 [../]
 [./fission_rate]
 [./burnup]
 [../]
 [./grain radius]
   initial_condition = 5.0e-6
 [../]
[Modules/TensorMechanics/Master]
 [./fuel]
                                                               View remainder of input file in editor.
   add variables = true
   strain = FINITE
```

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Questions?



11







TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

Running and Evaluating a Model in BISON

Running and Evaluating a Model in BISON

- Let's look at test/tests/triso/UCOElasticityTensor/UCOElasticityTensor.i.
- We will
 - Walk through the input file step by step.
 - 2. Run the file and review the information printed to the terminal.
 - Examine the CSV and Exodus output.

1. Review Input File

 In the terminal or an editor, view test/tests/triso/UCOElasticityTensor/UCOElasticityTensor.i

```
# Elastic Properties of UCO
# The geometry is a unit cube made of UCO material (initial density = 11.25 g/cm^3)
  400.00
            0.00E+00
                        0.00E+00
  470.00
# 610.00
# 680.00
[GlobalParams]
 displacements = 'disp_x disp_y disp_z'
 order = FIRST
  family = LAGRANGE
 initial_enrichment = 0.15 #[wt-]
 0 U = 1.5
 C U = 0.4
[Mesh]
  mesh
    type = GeneratedMeshGenerator
    xmax = 1.0
    ymax = 1.0
    zmax = 1.0
```

2. Run Input File

- First, compile bison-opt.
- > make
- Next, go to the directory containing the input file.
- > cd test/tests/triso/UCOElasticityTensor
- Finally, run the input file.
- > ../../../bison-opt -i UCOElasticityTensor.i
- Information to the terminal: BISON header and version, problem information, solve progress, and Postprocessor values.

3. Examine Results

- First, view the CSV file.
- > cat UCOElasticityTensor_out.csv
- Next, view the Exodus output file.
- There isn't one!
- Use the command line to add the Exodus output option.
- > ../../../bison-opt -i UCOElasticityTensor.i Outputs/exodus=true
- Load the Exodus output file in Paraview.
- > paraview UCOElasticityTensor_out.e

Questions?









TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

IAEA Benchmark Cases

[1] Hales, et al., JNM, 443, 2013.
 [2] Advances in high temperature gas cooled reactor fuel technology. Technical Report IAEA-TECDOC-1674, International Atomic Energy Agency, 2012.

IAEA Benchmark Cases

• IAEA cases studied in 2013 BISON TRISO paper:

| | Case | Geometry | Description | |
|--|-------------|------------|---|--|
| | 1 | SiC layer | Elastic only | |
| More complex material behavior, but fully prescribed. | 2 | IPyC layer | Elastic only Simple cases with analytical solutions | |
| | 3 | IPyC/SiC | Elastic with no fluence | |
| | f 4a | IPyC/SiC | Swelling and no creep | |
| | 4b | IPyC/SiC | Creep and no swelling | |
| | 4 c | IPyC/SiC | Creep and swelling | |
| | 4d | IPyC/SiC | Creep- and fluence-dependent swelling | |
| Single particle with realistic conditions. | 5 | TRISO | 350 µm kernel, real conditions | |
| | 6 | TRISO | 500 μm kernel, real conditions | |
| | 7 | TRISO | Same as 6 with high BAF PyC | |
| | 8 | TRISO | Same as 6 with cyclic temperature | |
| Internal | 10 | HFR-K3 | 10% FIMA, $5.3 \times 10^{-25} \text{n/m}^2$ fluence | |
| pressure set by | 11 | HFR-P4 | 14% FIMA, $7.2 \times 10^{-25} \text{ n/m}^2$ fluence | |
| FGR, CO production. | | | | |

2

IAEA Benchmarks from BISON TRISO JNM Paper

I.D. Hales et al./lournal of Nuclear Materials 443 (2013) 531-543

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the normal direction; and either the penetration distance or the contact force must be zero at all times.

In BISON, these contact constraints are enforced through the use of node/face constraints. Specifically, the nodes on one side of the interface are prevented from penetrating faces on the other side of the interface. This is a complished in a manner similar to that detailed by Heinstein and Laursen [37]. First, a geometric search determines which nodes have penetrated faces. For those nodes, the internal force computed by the divergence of stress is moved to the appropriate face at the point of contact. Those forces are distributed to the nodes attached to the face by employing finite element shave functions.

The tangential relationship between the contacting surfaces is modeled as free slip or frictionless.

2.4. Particle internal pressure

The pressure in the buffer and gap regions of the particle is computed based on the ideal gas law,

$$P = \frac{nRT}{V}$$
(28)

where P is the pressure, n is the moles of gas, R is the ideal gas constant, T is the temperature, and V is the gas-filled volume between the fuel and the IPyC layer. This pressure is applied to the surface of the buffer and to the inner surface of the IPyC layer.

The moles of gas, the temperature, and the cavity volume in this equation are free to change with time. The moles of gas n at any time is the original amount of gas (computed based on original pressure, temperature, and volume) plus the amount in the cavity due to fission gas released and carbon monoxide produced. The fission gas released is divided into 0.153 parts krypton and 0.847 parts xenon. The carbon monoxide production is based on oxygen production as described in Eq. (10).

The temperature T is taken as the average temperature of the buffer layer exterior and IPPC inner surfaces, brough any other measure of temperature could be used. It is assumed that initial porosity of the buffer layer is open and available to accommodate fission product gases and carbon monoxide. This initial volume prior to gao peering is computed by taking the volume of the buffer layer is one product gases and carbon monoxide. This initial volume prior to gao peering is computed by taking the volume of the buffer elevation was assumed to be the ratio of the buffer density to the IPPC density. The cavity volume V is recomputed as needed based on the evolving econometry.

The ideal gas law is used here for simplicity. It would be straightforward to implement a more complex law suitable for higher temperatures.

Table 1

IAEA CRP-6 benchmark cases considered in the BISON coated-particle verification exercise. HFR-K3 and HFR-P4 are German pebble and fuel element experiments,

| Case | Geometry | Description |
|------|------------|--|
| 1 | SiC layer | Elastic only |
| 2 | IPyC layer | Elastic only |
| 3 | IPyC/SiC | Elastic with no fluence |
| 4a | IPyC/SiC | Swelling and no creep |
| 4b | IPyC/SiC | Creep and no swelling |
| 4c | IPyC/SiC | Creep and swelling |
| 4d | IPvC/SiC | Creep- and fluence-dependent swelling |
| 5 | TRISO | 350 µm kernel, real conditions |
| 6 | TRISO | 500 µm kernel, real conditions |
| 7 | TRISO | Same as 6 with high BAF PvC |
| 8 | TRISO | Same as 6 with cyclic temperature |
| 10 | HFR-K3 | 10% FIMA, 5.3 × 10 ⁻²⁵ n/m ² fluence |
| 11 | HFR-P4 | 14% FIMA, 7.2 × 10 ⁻²⁵ n/m ² fluence |

3. Code verification

As part of an International Atomic Energy Agency (IAEA) Coordinated Research Program (IREA) on HTGR resort fuel technology, a set of benchmarking activities were developed to compare fuel performance codes under normal operation and operational transients [18]. Sixteen benchmark cases were identified, ranging in complexity from a simple fuel kernel having a single elastic coating layer, to realistic TRISO-coated particles under a variety of irradiation conditions. In each case, the particle geometry, constitutive relations, material properties and operating conditions were carefully prescribed to minimize differences between the various code predictions; details are given in [18]. As an early code verification exercise, BISON has been applied to 13 of the 16 benchmark cases as summarized in Table 1.

In the present study, the models for all benchmark cases use eight quadratic finite elements across the width of each coating layer. For cases 1 and 2, numerical solutions were also obtained with twelve elements across the coating layer to determine whether the mesh was sufficiently refined. Maximum tangential stresses obtained from the eight- and twelve-element models differed at most by 0.1% demonstrating adequate mesh convergence with eight elements.

Cases 1–3 were limited to single and double coating layers and tested simple elastic thermomechanical behavior against analytical solutions. A comparison of the analytical and BISON numerical solutions for the maximum tangential stress, which occurs at the inner surface of the various layers is shown in Table 2. Comparisons are excelled.

Cases 4a–4d included both IPVC and Sic layers and investigated pryorlytic carbon layer behavior under avariety of conditions. Cases 5–8 considered a single TRISO particle with more complexity added with each subsequent case. For cases 1–4d, the internal gas pressure was fixed at 25 MPa while cases 5–8 included a linear pressure ramp. The particle temperature was held uniform at 1273 K for cases 1–7, but for case 8 was sycled ten times between 873 and 1278 K, characteristic of fine lin a pebble bed reactor, For cases 4–7, Table 3 compares BISON computed solutions to the range of solutions from eight coarded-particle fled codes included in the CRP-6 exercise (see [18]). Comparisons are of the tangential stress at the inner surface of both the IPVC and SiC Jayers, at the end of irradiation. The BISON solutions are always within the range defining the ranges were extracted from plots in [18] and are thus not never the conditions of the surface of the codes included defining the ranges were extracted from plots in [18] and are thus not never the code of the code

Although code comparisons in Table 3 are provided only at the end of irradiation, comparisons were made at various intermediate times during the irradiation period. The BISON solutions were always within the range of solutions produced by the CRP-6 codes.

Fig. 3 compares solutions for case 8, which involved a cyclic particle temperature, during the full irradiation history. In this figure, BISON solutions of the tangential stress at the inner wall of the IPVC and SCI. layers are compared to solutions from three codes from the CRP-6 exercise, namely PARFUME [11], ATIAS [15] and STRESS3 [38]. As above, data for the code comparisons were extracted from plots in [18]. For the IPVC layer, the four solutions essentially overlay each other during the entire irradiation period.

Table 2
Comparison of the BISON computed maximum tangential stress (MPa) to the analytical solution for Cases 1-3

| unuiyacur s | Judion for Cases | | | |
|-------------|------------------|------------|-----------|-----------|
| Case | Layer | Analytical | BISON | Error (%) |
| 1 | SiC | 125.19 | 125.23 | 0.032 |
| 2 | IPyC | 50.200 | 50.287 | 0.173 |
| 3 | IPyC/SiC | 8.8/104.4 | 8.7/104.5 | 1.14/0.10 |

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Table 3

Comparison of the BISON computed tangential stress (MPa) to the range of values computed by the codes included in the CRP-6 exercise. Comparisons are at the inner

| Case | Layer | CRP-6 codes [range] | BISON |
|------|----------|-----------------------|------------|
| ŧa | IPyC/SiC | [925,970]/[-775,-850] | 928/-819 |
| 4b | IPyC/SiC | [-25, -25]/[138, 142] | -25.0/139 |
| 4c | IPyC/SiC | [25,27]/[83,92] | 26.0/89.4 |
| 4d | IPyC/SiC | [25,35]/[71,88] | 27.8/87.0 |
| 5 | IPyC/SiC | [40,58]/[-56,-28] | 41.9/-32.2 |
| 6 | IPyC/SiC | [27,38]/[28,48] | 29.2/44.9 |
| 7 | IPyC/SiC | [37,50]/[10,25] | 38.0/24.6 |

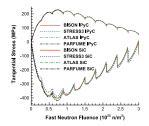


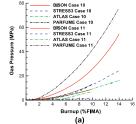
Fig. 3. Code comparison for case 8, which included a ten cycle temperature history Plotted is the tangential stress at the inner wall of the IPyC and SiC layers.

In the SiC layer, the four solutions are quite similar but some differences are evident, particularly for the first four temperature cycles. The BISON solution falls roughly midway between the PARPUME and STRESS3 solutions and is essentially identical to the ATLAS solution.

Cases 9-13 in CRP-5 were more complicated benchmarks based on past or planned experiments with TRISO-casted particles. The two cases considered here (10 and 11) were based on German fuel from pebble and fuel element experiments. Again, details are provided in [18]. Although material properties and constitutive relations were prescribed for these cases, they differed from cases 1-8 in two ways; (1) the internal pressure was not fixed but instead determined by fission gas release and CO production and (2) the particle size was prescribed as a population (mean value and standard deviation) rather than a single value. BISON solutions were based on the gas release and CO production models described above; however, for simplicity, only a single particle size was considered based on the mean particle diameter.

Fig. 4 provides code comparisons of the total gas pressure (Fig. 4a) and tangential stress at the inner wall of the SiC layer (Fig. 4b) for benchmark cases 10 and 11. Again, BlSON is compared to three codes from the CRP-6 exercise. Substantial differences exist in these solutions, particularly for the gas pressure. The BISON solution histories, however, compare well to the range of solutions given by the three well-established codes: chosen for romanization.

As stated in [18], the differences between various code predictions shown in Figs. 4a and 4b can be largely attributed to the models used to calculate fission gas release and CO production in the kernel. A detailed description of these models is not available in [18], limiting more detailed investigation. One obvious and significant difference is that both BIOSM and ATIAS employ the simple Proksch et al. [34] empirical model for CO production while PAR-EIME III uses a detailed themschemical model.



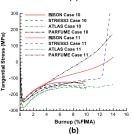


Fig. 4. Code comparisons of the total gas pressure (a) and tangential stress at the inner wall of the SiC layer (b) for benchmark cases 10 and 11.

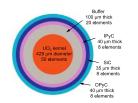


Fig. 5. Schematic showing the particle geometry assumed in the model. For a 1D mesh, the number of finite elements used in each layer is indicated.

4. Demonstration problems

Three problems are considered to demonstrate BISON applicability to coated-particle fuel. The first is a 1D spherically symmetric TRISO-coated particle evaluated during periods of normal irradiation, storage, and accident testing. The second problem considers

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Explore the Benchmark Cases

Questions?



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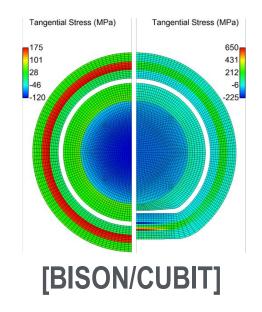


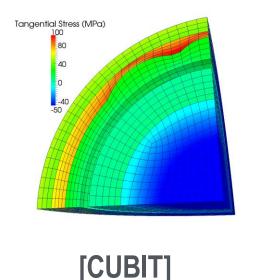
TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory Meshing

Mesh Generation

- Clearly mesh generation depends on the type of analysis to be run.
 - 1D (fast, spherically symmetric)
 - 2D (medium, axisymmetric)
 - 3D (slow, symmetry across planes or not symmetric)





[BISON]

TRISO 1D Mesh

Creates a 1D mesh for use with TRISO analysis

Description

Creates a 1D mesh appropriate for use in TRISO analysis. The user supplies radial coordinates that mark the boundaries of mesh blocks. A list of numbers of elements per block is also supplied. Sidesets are created at each mesh boundary.

Example Input Syntax

```
[Mesh]
  type = TRISO1DMesh
  elem_type = EDGE2
  coordinates = '0 .1 .1 .2'
  mesh_density = '1 0 2'
  block_names = 'fred wilma'
[]
```

(test/tests/triso/mesh/mesh_with_coincident_nodes.i)

Input Parameters

Required Parameters

Screenshot from

https://mooseframework.org/bison/source/mesh/TRISO1DMesh.html

```
coordinates Radial coordinates of mesh block boundaries.

mesh_density A list giving the number of elements in each interval (could be zero for a gap).
```

Optional Parameters

```
allow_renumbering (True) If allow_renumbering=false, node and element numbers are kept fixed until ...

block_names A list of names to be assigned to the mesh blocks.

elem_type (EDGE3) The type of element from libMesh to generate

ghosting_patch_size The number of nearest neighbors considered for ghosting purposes when 'iterati...

max_leaf_size (10) The maximum number of points in each leaf of the KDTree used in the nearest neigh...

parallel_type (DEFAULT) DEFAULT: Use libMesh::ReplicatedMesh unless --distributed-mesh is specifi...
```

Example BISON Documentation File

- Mesh generation for 1D TRISO in BISON is done using TRISO1DMesh.
- TRISO1DMesh supports an arbitrary number of layers.

```
[Mesh]
  type = TRISO1DMesh
  elem_type = EDGE3
  coordinates = '0 2.485e-4 3.425e-4 3.425e-4
3.835e-4 4.195e-4 4.595e-4'
  mesh_density = '6 6 0 6 8 6'
  block_names = 'fuel buffer IPyC SiC OPyC'
[]
```

(See assessment/TRISO/benchmark/IAEA_CRP-6/case_11/case_11_1D.i)

Run Case 11.

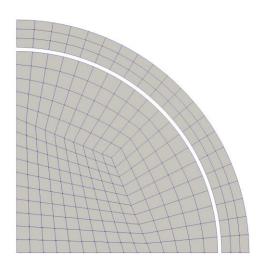
```
> cd assessment/TRISO/benchmark/IAEA_CRP-6/case_11
> ../../../bison-opt -i case_11_1D.i
```

View mesh for Case 11.

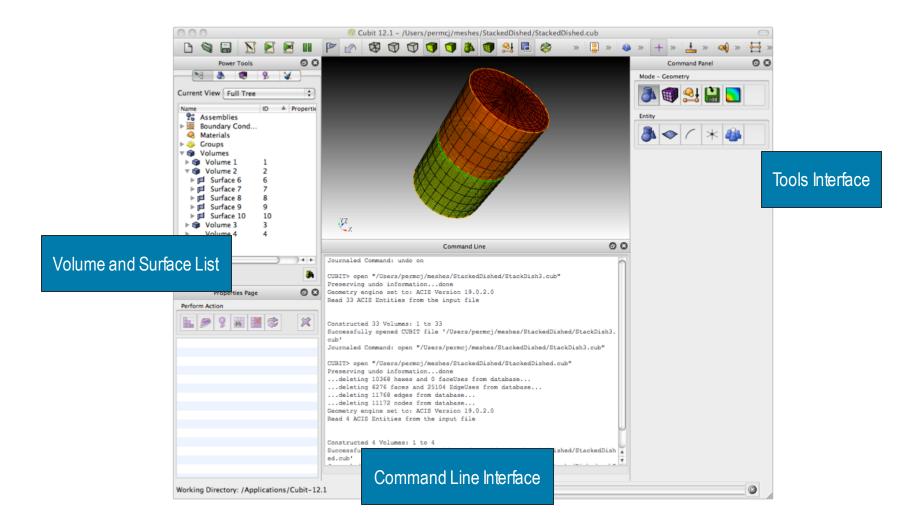
```
> paraview case 11 1D out.e
```

- Orient –Z.
- Change line width.
- Note block names and sideset names.

- CircularCrossSectionMesh will create quarter- or halfcircle meshes for axisymmetric analysis.
- This tool was built with LWR fuel in mind but can be used for TRISO meshes.
- This tool is a bit more involved. See the documentation pages and tests for more information.



Mesh Generation with CUBIT



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Questions?



9







TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

TRISO Thermal Models

TRISO Thermal Models

 Thermal modeling for TRISO fuel follows the same pattern as for any other fuel:

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + E_f \dot{F}$$

- That is, we need to
 - Define density, specific heat, and thermal conductivity, which may be functions of temperature or other parameters.
 - Invoke the heat conduction and heat conduction time derivative kernels.

Thermal Material Properties

Often, thermal properties are specified as constants.

```
[Materials]
 [./SiC_elasticity_tensor]
   type = ComputeIsotropicElasticityTensor
   block = SiC
   youngs modulus = 3.7e11
   poissons ratio = 0.13
 [../]
 [./SiC elastic stress]
   type = ComputeFiniteStrainElasticStress
   block = SiC
  [./SiC_temp]
   type = HeatConductionMaterial
   block = SiC
   thermal_conductivity = 13.9
                                   # J/m-s-K
   specific heat = 620.0
                                         # J/ka-K
 [../]
  [./SiC den]
   type = Density
   density = 3180.0
                                         # kg/m^3
   block = SiC
 [.../]
```

Thermal Material Properties Continued

Thermal properties may also be computed in a Material object.

```
[./fuel_thermal]
  type = ThermalFuel
  thermal_conductivity_model = FINK_LUCUTA
  block = fuel
  temp = temp
  burnup = burnup
  initial_porosity = 0.0
[../]
AEA cases studied in 2013 BISON TRISO paper.
```

Thermal Kernels

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Questions?



3







TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

TRISO Mechanical Models

TRISO Mechanical Models

 Mechanical modeling for TRISO fuel follows the same pattern as for any other fuel:

$$\nabla \cdot \mathbf{T} + \rho \mathbf{f} = 0$$

- This is more involved than thermal modeling.
 - 1. Define constitutive response (define, e.g., an elasticity tensor and an object to convert strain to stress).
 - 2. Define so-called eigenstrains (thermal strain, irradiation strain)
- The code provides input shortcuts to invoke the computation of strain and the divergence of stress. This shortcut may or may not be used.

Simple Elasticity

```
[Materials]
 [./SiC_elasticity_tensor]
   type = ComputeIsotropicElasticityTensor
   block = SiC
   youngs_modulus = 3.7e11
   poissons_ratio = 0.13
 [../]
  [./SiC_elastic_stress]
   type = ComputeFiniteStrainElasticStress
   block = SiC
 [../]
  [./SiC_temp]
   type = HeatConductionMaterial
   block = SiC
   thermal_conductivity = 13.9 # J/m-s-K
   specific_heat = 620.0
                                        # J/kg-K
  [../]
  [./SiC_den]
   type = Density
   density = 3180.0
                                         # kg/m^3
   block = SiC
 [../]
```

Creep

```
[Materials]
 [./IPyC_elasticity_tensor]
   type = ComputeIsotropicElasticityTensor
   block = IPyC
   youngs_modulus = 3.96e10
   poissons_ratio = 0.33
 [.../]
 [./IPyC_stress]
   type = PyCCreep
   block = IPyC
   flux = fast_neutron_flux
   temperature = temp
   density = 1900.0
                                         # kg/m^3
 [.../]
 [./IPyC_temp]
   type = HeatConductionMaterial
   block = IPyC
   thermal_conductivity = 4.0 # J/m-s-K
   specific_heat = 720.0
                                        # J/kg-K
 [.../]
 [./IPyC_den]
   type = Density
   density = 1900.0
   block = IPyC
```

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Creep + Irradiation Strain

```
[Materials]
 [./IPyC_elasticity_tensor]
   type = ComputeIsotropicElasticityTensor
   block = IPyC
   youngs_modulus = 3.96e10
   poissons ratio = 0.33
 [.../]
 [./IPyC stress]
   type = PyCCreep
   block = IPyC
   flux = fast neutron flux
   temperature = temp
   density = 1900.0
                                         # kg/m^3
 [.../]
 [./IPyC_temp]
   type = HeatConductionMaterial
   block = IPyC
   thermal_conductivity = 4.0 # J/m-s-K
   specific heat = 720.0
                                    # J/kg-K
 [.../]
 [./IPyC_den]
   type = Density
   density = 1900.0
   block = IPyC
 [../]
 [./IPyC_densification]
   type = PyCIrradiationEigenstrain
   block = IPyC
   fluence = fluence
   pyc_type = dense
   eigenstrain name = IPyC eigenstrain
 [../]
```

Shortcut for Strain and Divergence of Stress

```
[Modules/TensorMechanics/Master]
use_displaced_mesh = true
generate_output = 'stress_xx stress_yy stress_zz stress_xy stress_zx hydrostatic_stress'
strain = FINITE
incremental = true
add_variables = false
[./default]
block = 'fuel buffer IPyC OPyC'
eigenstrain_names = 'thermal_strain swelling_strain'
[../]
[./SiC]
block = 'SiC'
eigenstrain_names = 'thermal_strain'
[../]
[]
```

Screenshot from examples/TRISO/accident simulation/triso2D accident.i

With No Shortcut for Strain and Divergence of Stress

```
[Kernels]
  [./TensorMechanics]
   use_displaced_mesh = true
  [../]
```

```
[Materials]
 [./fission_gas_release]
                                       # Sifgr fission gas release mode
   type = Sifgrs
   block = fuel
   temp = temp
   fission rate = fission rate
                                       # coupling to fission rate aux variable
   grain_radius_const = 5.0e-6
 [../]
 [./stress]
   type = ComputeLinearElasticStress
   block = 'fuel buffer SiC'
 [../]
 [./strain]
   type = ComputeRSphericalSmallStrain
   block = 'fuel buffer SiC'
   eigenstrain_names = thermal_strain
```

TRISO Mechanical Models in BISON

- UCO
 - UCOElasticityTensor
 - UCOVolumetricSwellingEigenstrain
- PyC/Buffer
 - PyCElasticityTensor
 - PyCIrradiationEigenstrain
 - PyCCreep
- If the material requires only linear elasticity and thermal expansion, no specialized models are required.

Questions?



9







TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

Fission Gas and Internal Pressure

Fission Gas Production and Release for TRISO Fuel

- BISON provides two models for fission gas production and release:
 - 1. Sifgrs

https://mooseframework.org/bison/source/materials/Sifgrs.html

- For use with UO₂.
- Used in all our LWR cases.
- 2. UCOFGR
 - For use with UCO.
 - New model developed in cooperation with Kairos Power.

Too new but will be at

https://mooseframework.org/bison/source/materials/UCOFGR.html

Can build our own...

Sifgrs

```
[Materials]
 [./fission_gas_release]
                                      # Sifgr fission gas release mode
   type = Sifgrs
   block = fuel
   temp = temp
   fission rate = fission rate
   grain_radius_const = 5.0e-6
 [../]
 [./stress]
   type = ComputeLinearElasticStress
   block = 'fuel buffer SiC'
 [../]
 [./strain]
   type = ComputeRSphericalSmallStrain
   block = 'fuel buffer SiC'
   eigenstrain_names = thermal_strain
 [.../]
```

```
[Postprocessors]
[./fis_gas_released]  # fission gas_released to plenum (moles)
    type = ElementIntegralFisGasReleasedSifgrs
    block = fuel
    execute_on = 'initial linear nonlinear timestep_begin timestep_end'
[../]
```

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UCOFGR

```
[Materials]
  [./burnup]
   type = GenericFunctionMaterial
   prop_names = burnup
   prop values = burnup
  [./thermal]
   type = HeatConductionMaterial
   block = '1'
   thermal conductivity = 1.0
   specific heat = 1.0
   temp = temp
  [../]
  [./fission_gas_release]
   type = UCOFGR
   block = '1'
   average_grain_radius = 10e-6
   triso_geometry = particle_geometry
   temperature = temp
   fission_rate = fission_rate
 [../]
```

Can use ElementIntegralMaterialProperty
Postprocessor to compute fission gas
produced (fis_gas_produced) and fission
gas released (fis_gas_released).

Internal Pressure

- BISON uses the ideal gas law to compute internal pressure.
- The PlenumPressure object was built for use with LWRs, but it works just as well for TRISO.
- It is a boundary condition and appears in the BCs area of the input file.
- We must supply:
 - Volume (a Postprocessor value)
 - Gas temperature (a Postprocessor value)
 - Initial pressure (a raw number; used to compute initial moles of gas)
 - Added moles of gas over time (one or more Postprocessor values)

PlenumPressure

```
[./PlenumPressure] # apply plenum pressure on clad inner walls and pellet surfaces
  [./plenumPressure]
   boundary = BufferGapVol
   initial pressure = 0
   startup_time = 1.0e4
    R = 8.3143
   output_initial_moles = initial_moles
   temperature = ave temp interior
   volume = volumeGas
                                                       # coupling to post processor to get gas volume
   material input = 'fis gas released co production'
                                                       # coupling to post processor to get fission gas added, co added
   output = plenum_pressure
                                                       # coupling to post processor to output plenum/gap pressure
  [../]
[../]
```

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InternalVolume

InternalVolume is a Postprocessor

```
[./volumeGas]
  type = InternalVolume
  boundary = BufferGapVol
# ro = 3.125e-4
# ri = 2.125e-4
# vb = 4/3*pi*(ro^3-ri^3) = 8.76e-11
# buffer density = 1000
# PyC density = 1900
# fill ratio = 10/19
# vb*10/19 = 4.6e-11
# Must remove 4.6e-11 m^3 from the volume
  addition = -4.6e-11
  execute_on = 'initial linear nonlinear timestep_begin timestep_end'
[../]
```

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Gas Temperature

For the gas temperature, we use SideAverageValue

```
[./ave_temp_interior]
  type = SideAverageValue
  boundary = BufferGapVol
  variable = temp
  execute_on = 'initial linear nonlinear timestep_begin timestep_end'
[../]
```

Added Moles of Gas

If using Sifgrs:

```
[./fis_gas_released]  # fission gas released to plenum (moles)
  type = ElementIntegralFisGasReleasedSifgrs
  block = fuel
  execute_on = 'initial linear nonlinear timestep_begin timestep_end'
[../]
```

For CO production with UO₂ fuel:

```
[./co_production]
  type = CarbonMonoxideProduction
  total_fissions = total_fissions
  time_int_surf_temp = time_int_surf_temp
  execute_on = 'initial linear nonlinear timestep_begin timestep_end'
[../]
```

Questions?



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TRISO in BISON

Computational Mechanics and Materials Idaho National Laboratory

Fission Product Diffusion

TRISO Fission Product Diffusion Models

 Fission product diffusion modeling for TRISO fuel follows the same pattern as for any other fuel:

$$\frac{\partial C}{\partial t} = \nabla \cdot D \left(\nabla C - \frac{CQ^*}{FRT^2} \nabla T \right) - \lambda C + S$$

- That is, we need to
 - Define diffusion coefficient D.
 - 2. Define Soret coefficients (if used).
 - 3. Define decay (C) and source (S) terms.
 - 4. Invoke the diffusion kernels.

Screenshots that follow are from examples/TRISO/accident_simulation/triso2D_accident.i

Define Diffusion Coefficient Material Properties

```
[./SiC_conc]
 type = ArrheniusDiffusionCoef
 block = SiC
 d1 = 5.5e-14
                                # m^2/s
 d1 function = d1 function
 d1 function variable = fluence
 q1 = 125.0e+3
                                # J/mol
 d2 = 1.6e-2
                                # m^2/s
 q2 = 514.0e+3
                                # J/mol
 gas constant = 8.3143
                                # J/K-mol
 temp = temp
[../]
```

Be sure to define coefficient for each material.

Invoke Decay, Source, and Diffusion Kernels

```
[Kernels]
 [./heat_ie]
   type = HeatConductionTimeDerivative
   variable = temp
 [../]
 [./heat]
   type = HeatConduction
   variable = temp
 [../]
 [./heat_source]
    type = NeutronHeatSource
    variable = temp
    block = fuel
    energy per fission = 3.2e-11 # units of J/fission
    fission rate = fission rate
 [../]
 [./mass_ie]
   type = TimeDerivative
   variable = conc
 [../]
 [./mass]
   type = ArrheniusDiffusion
   variable = conc
 [.../]
 [./mass_source]
   type = BodyForce
   variable = conc
   function = power history
   value = 1.22e-5 # units of moles/m**3-s
   block = fuel
 [../]
 [./mass_decay]
   type = Decay
   variable = conc
   radioactive decay constant = 7.297e-10 # units: (1/sec) The constant for Cesium
 [.../]
```

Questions?



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