



Hybrid Temperature-Reactivity PID Controllers for Nuclear Thermal Propulsion Startup

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Changing the World's Energy Future

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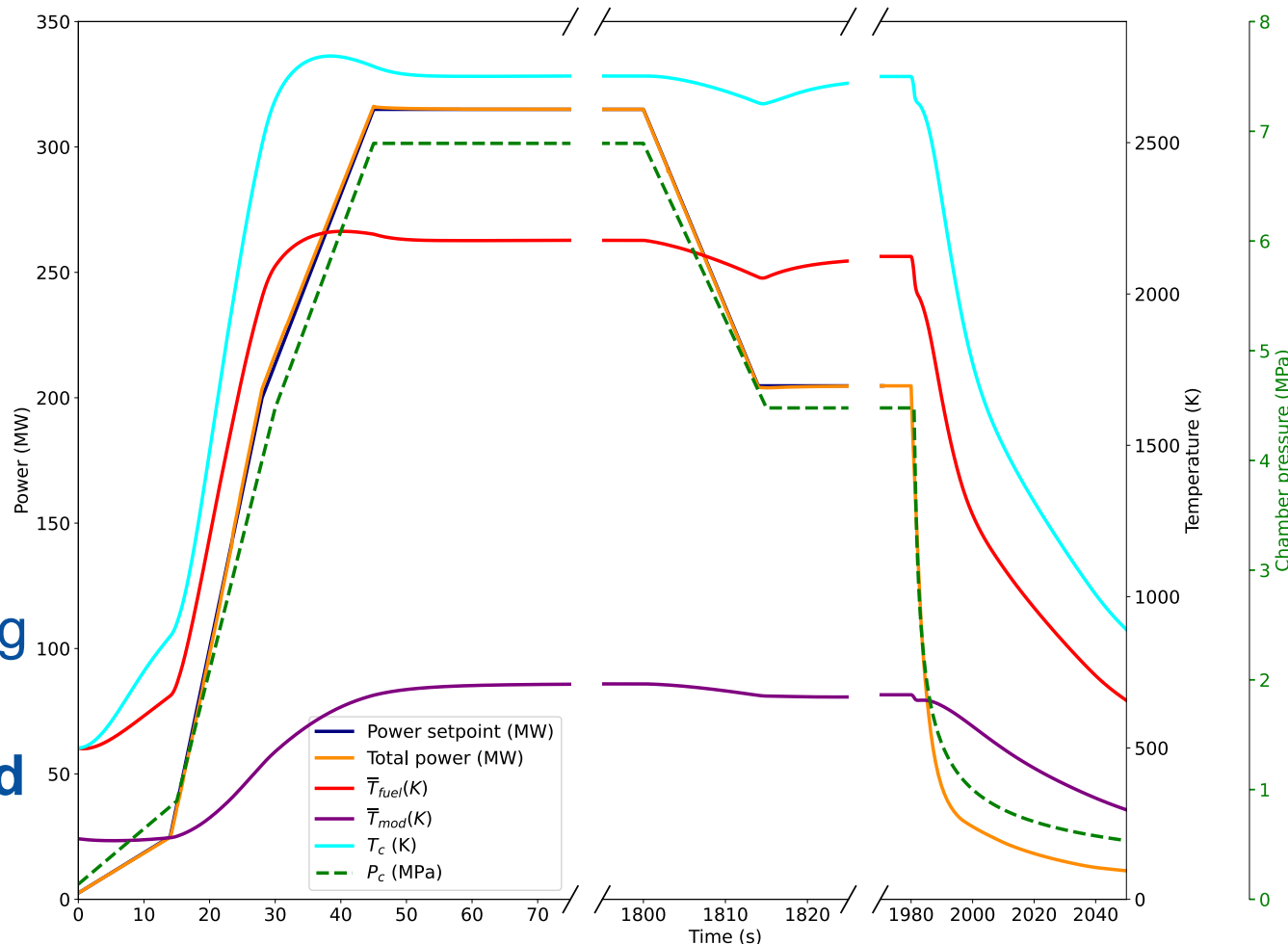
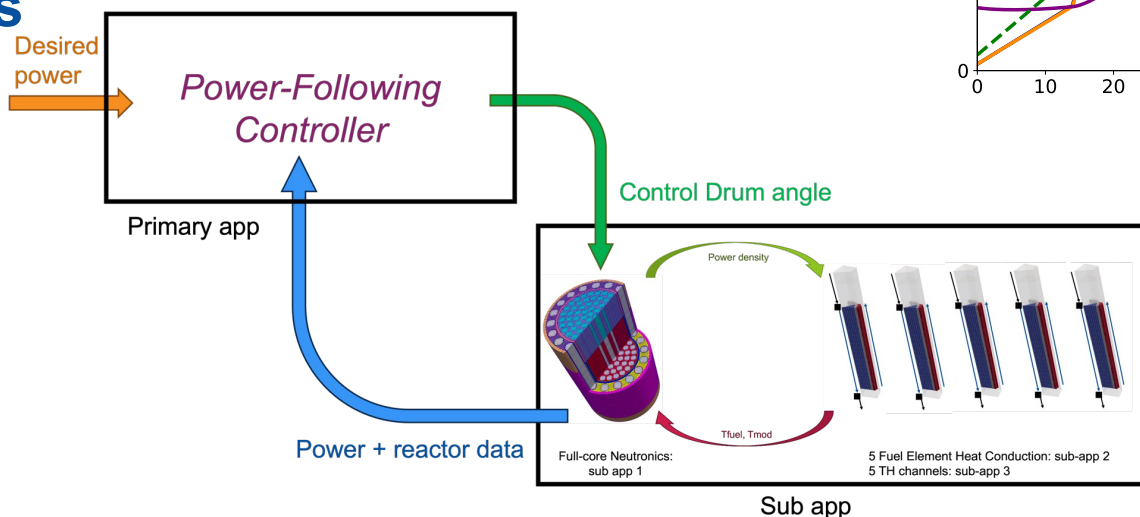


Outline

- Motivation
- Simplified Model
- Temperature/Reactivity Control
- Future Work

Motivation

- Pressure/mass flow rate as BC
- Pre-defined power setpoint
- Good controller response
- Temperature overshoot ($\sim 3\%$) and not constant during throttling because not using a temperature demand
- **Goal: investigate temperature-controlled systems**



Source: V. Labouré, S. Schunert, S. Terlizzi, Z. Prince, J. Ortensi, C-S Lin, L. Charlot, and M. DeHart, "Automated Power-following Control for Nuclear Thermal Propulsion Startup and Shutdown Using MOOSE-based Applications", accepted by Progress in Nuclear Energy in April 2023.

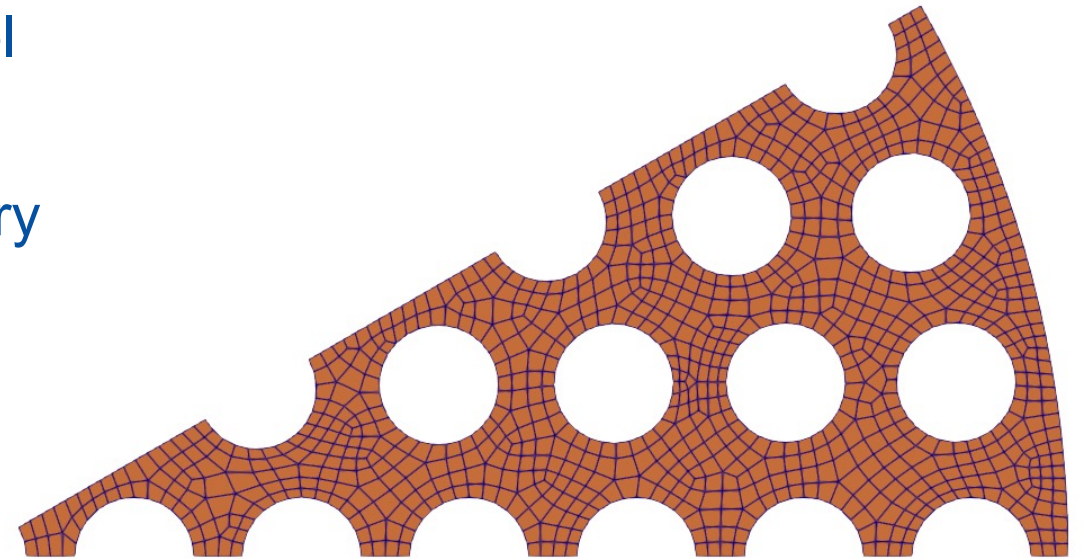
Multiphysics Model

- Simplified PKE model with fixed reactivity coefficients and prototypical kinetics parameters
- Single 3-D representative fuel element with heat conduction and convection at cooling channel boundary
- Single 1-D representative fuel cooling channel
- Chamber temperature (T_c) used for control
- Chamber pressure (P_c) prescribed as boundary condition and mass flow rate given by:

$$\dot{m}(t) = \frac{\dot{m}_{nom} \sqrt{T_{c,nom}}}{P_{c,nom}} \frac{P_c(t)}{\sqrt{T_c(t)}}$$

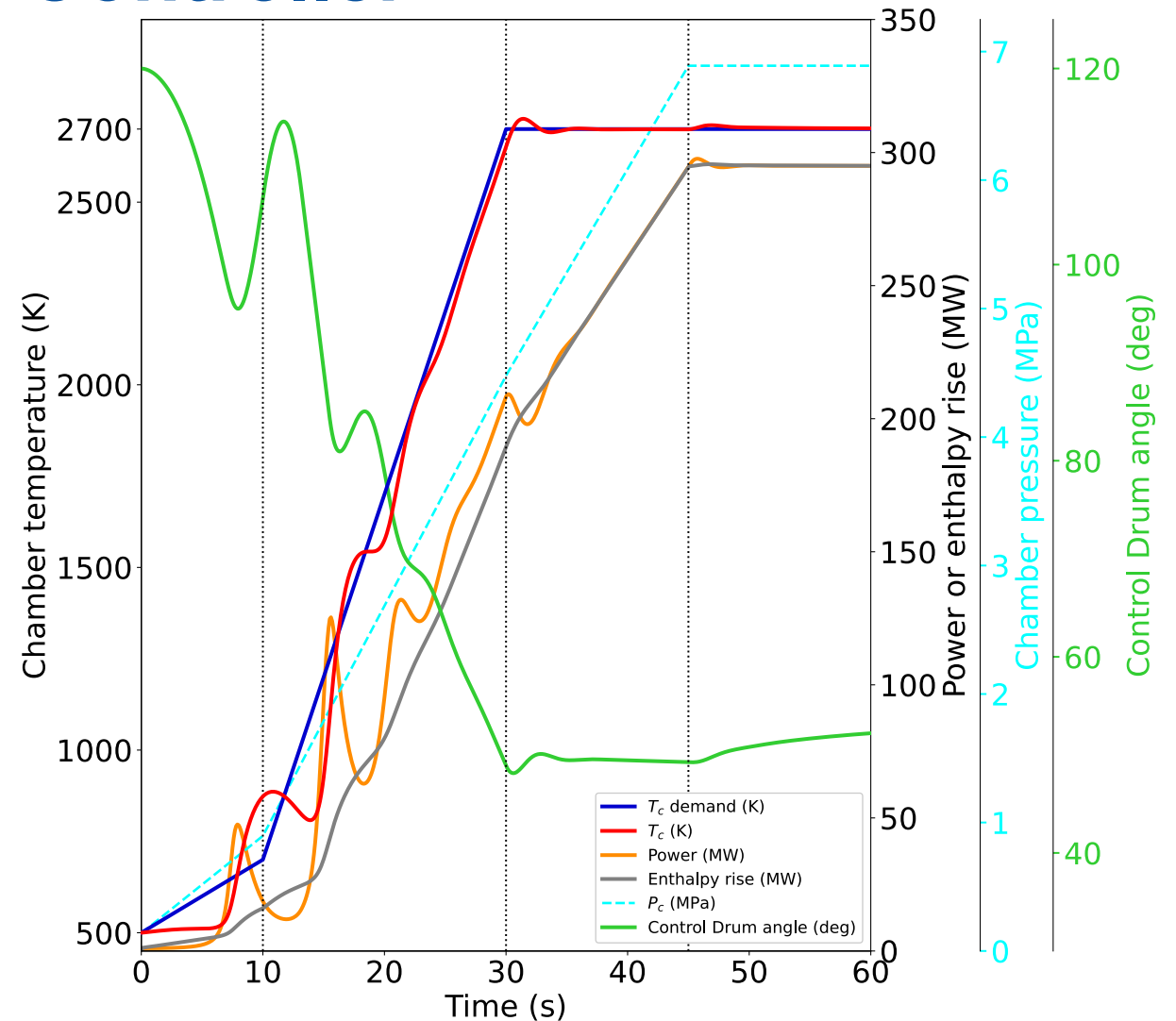
TABLE I. Kinetics parameters used in the neutronics model. λ_i and β_i are the delayed neutron decay constants and fractions, respectively. Λ is the mean generation time.

Delayed Group	λ_i (s ⁻¹)	β_i (pcm)	Λ (s)
1	1.3346×10^{-2}	24.6	1.33×10^{-5}
2	3.2667×10^{-2}	128.6	
3	1.2094×10^{-1}	124.3	
4	3.0444×10^{-1}	282.0	
5	8.5639×10^{-1}	121.7	
6	2.8764×10^0	50.8	
Sum		732.1	



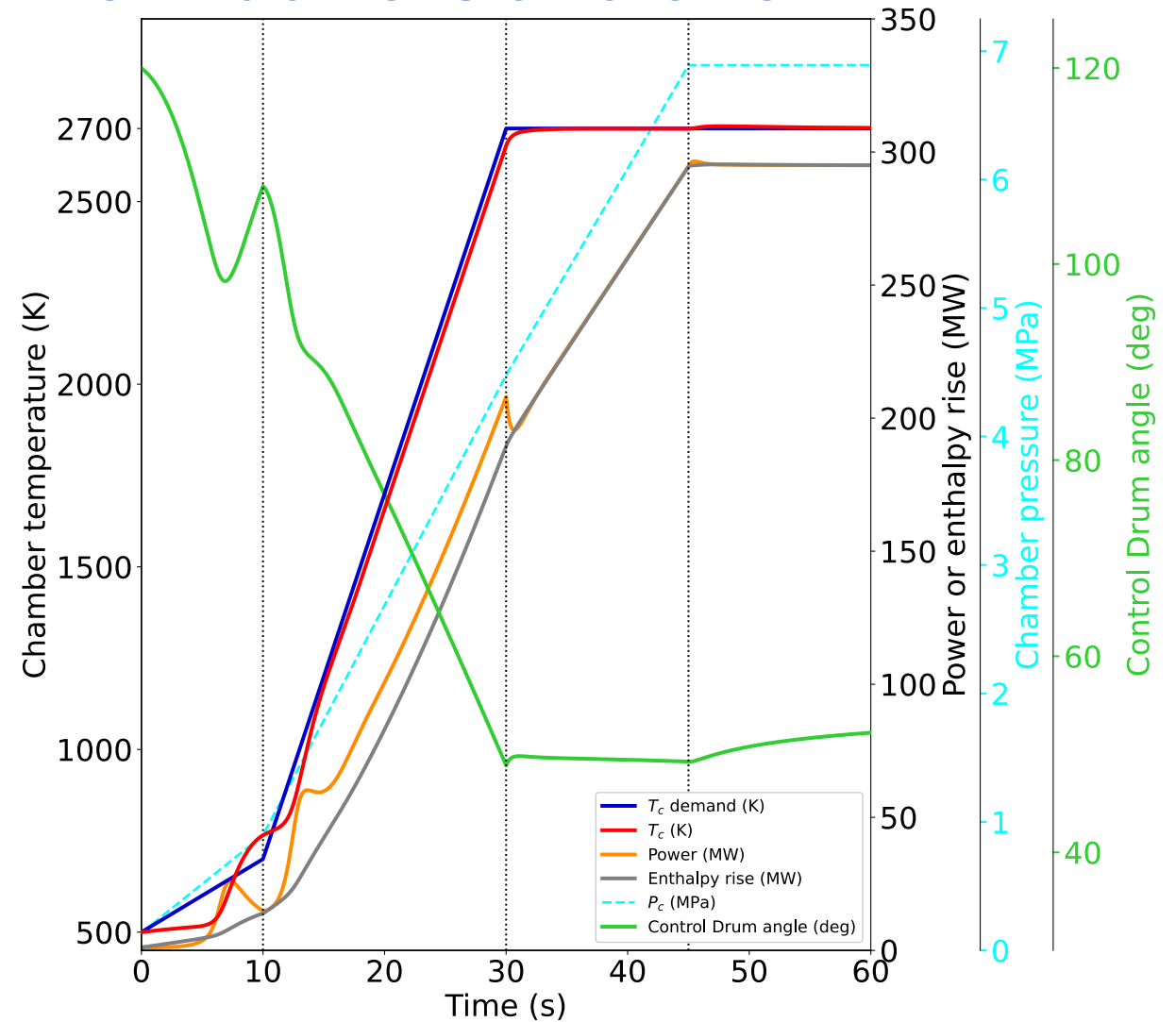
Temperature Proportional Controller

- Drums controlled by directly comparing the predicted and desired chamber temperatures
- Oscillatory behavior due to delay between drum rotation and chamber temperature rise
- Initial response quite slow
- Temperature overshoot



Temperature Proportional-Derivative Controller

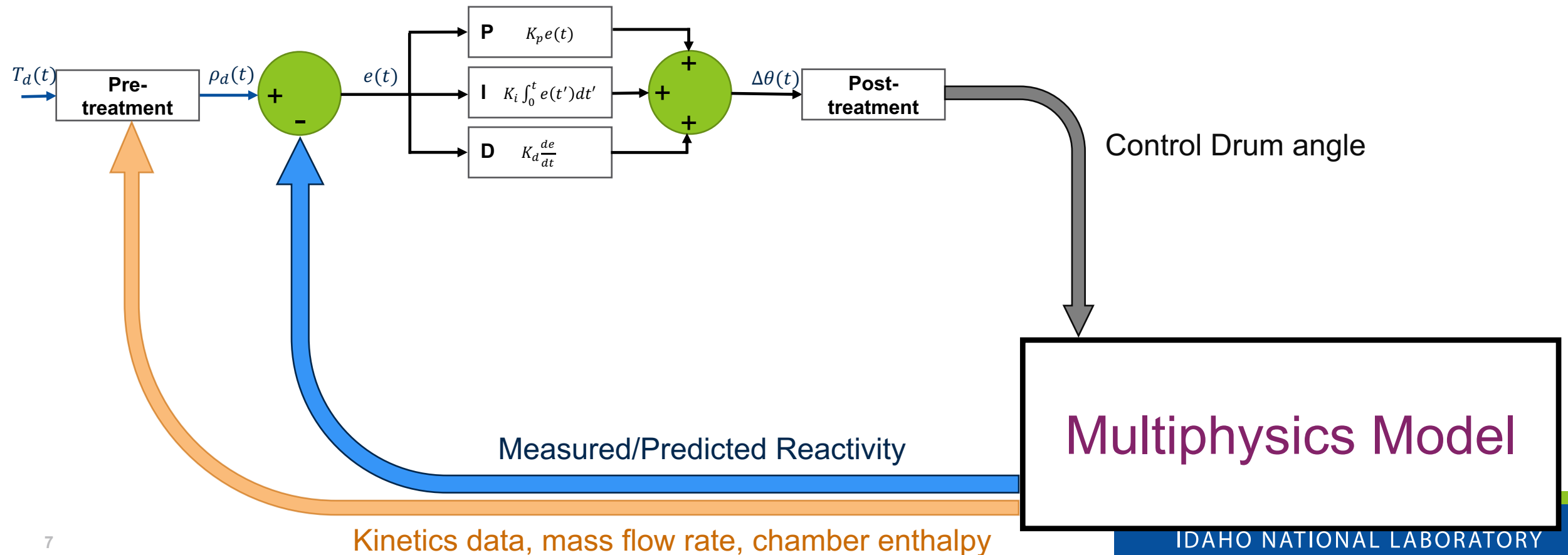
- Derivative term (i.e., anticipation) included
- Much smoother behavior
- Initial response still slow/oscillatory
- But overall behavior much better
- Caveat: derivative component would require noise filtering



Reactivity Controller

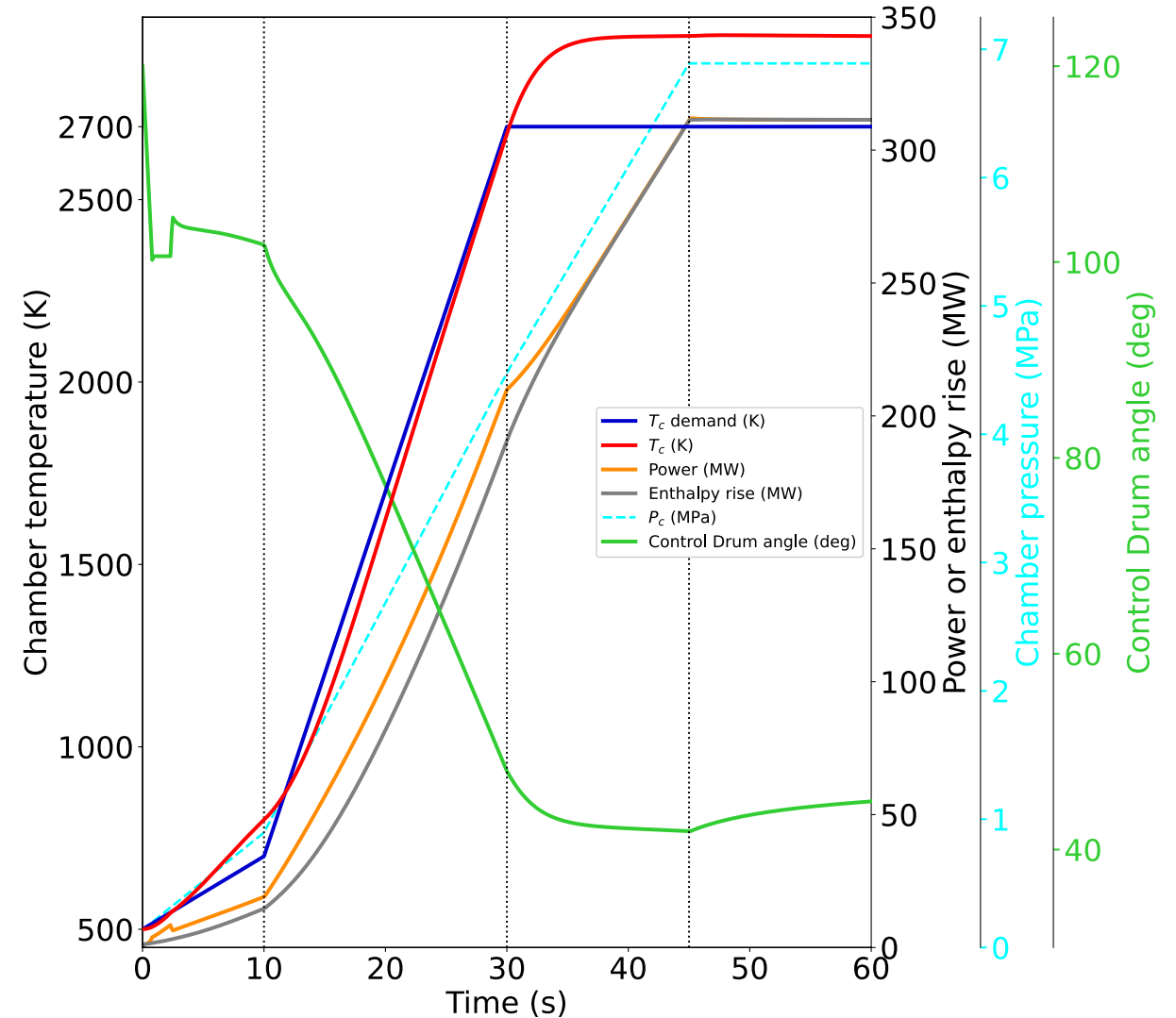
$$\begin{cases} \mathcal{P}_d \approx \dot{m}(H_{out}(T_d) - H_{tank}) \\ \rho_d = \frac{\Lambda}{\mathcal{P}_d \beta_{eff}} \left(\frac{d\mathcal{P}_d}{dt} - \sum_i \lambda_i C_i \right) + 1 \end{cases}$$

- Pre-treatment to convert temperature demand to reactivity demand
- Post-treatment to make sure the CDs do not exceed a certain speed (25 deg/s) and reactor period stays above 2.5 s



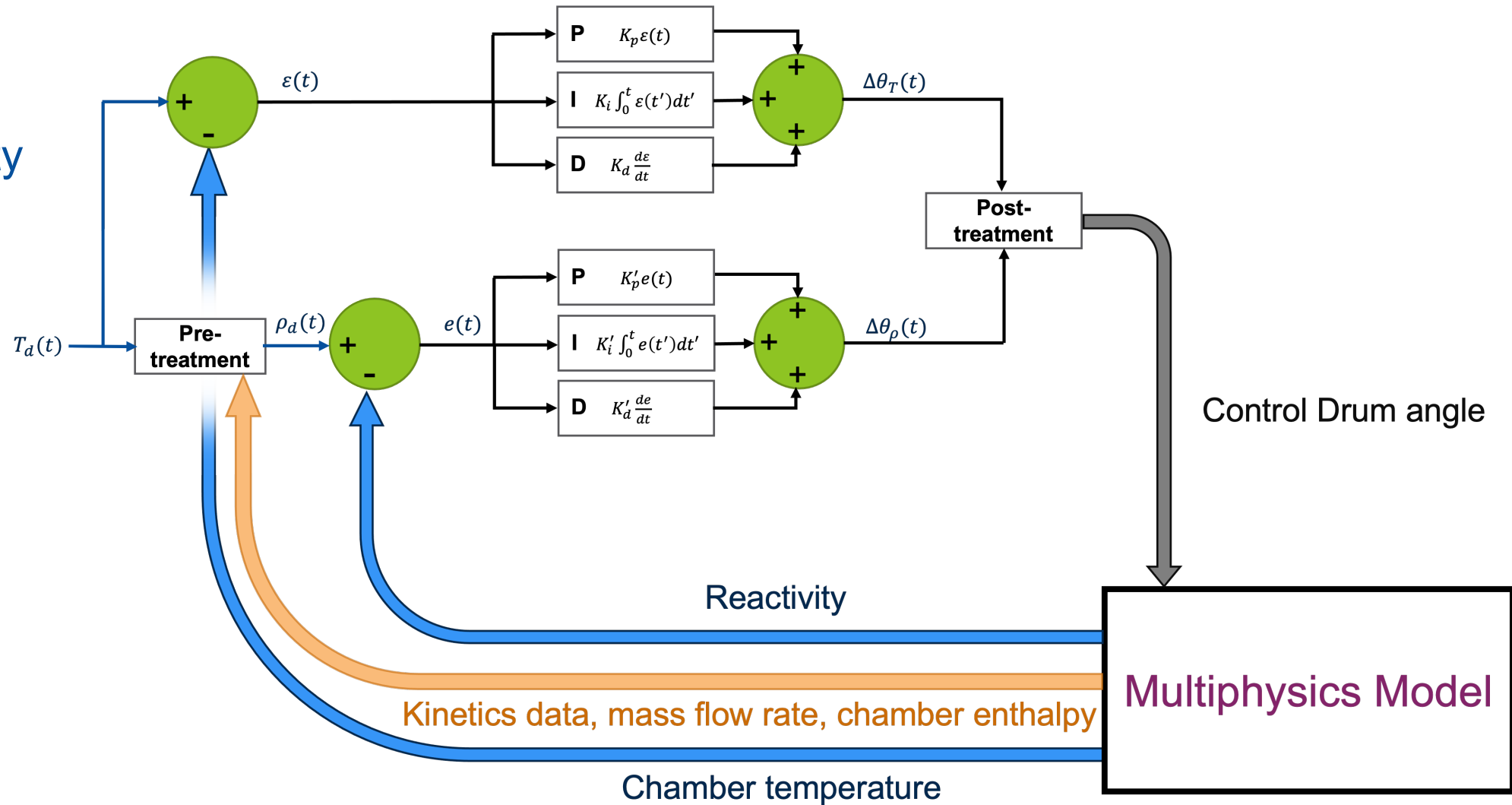
Reactivity Proportional Controller

- Faster initial response
- Initially, CD speed limited and set to 0 when the period goes lower than 2.5 s
- But T_c does not stabilize to the desired temperature because of inexact conversion $T_d \rightarrow \rho_d$



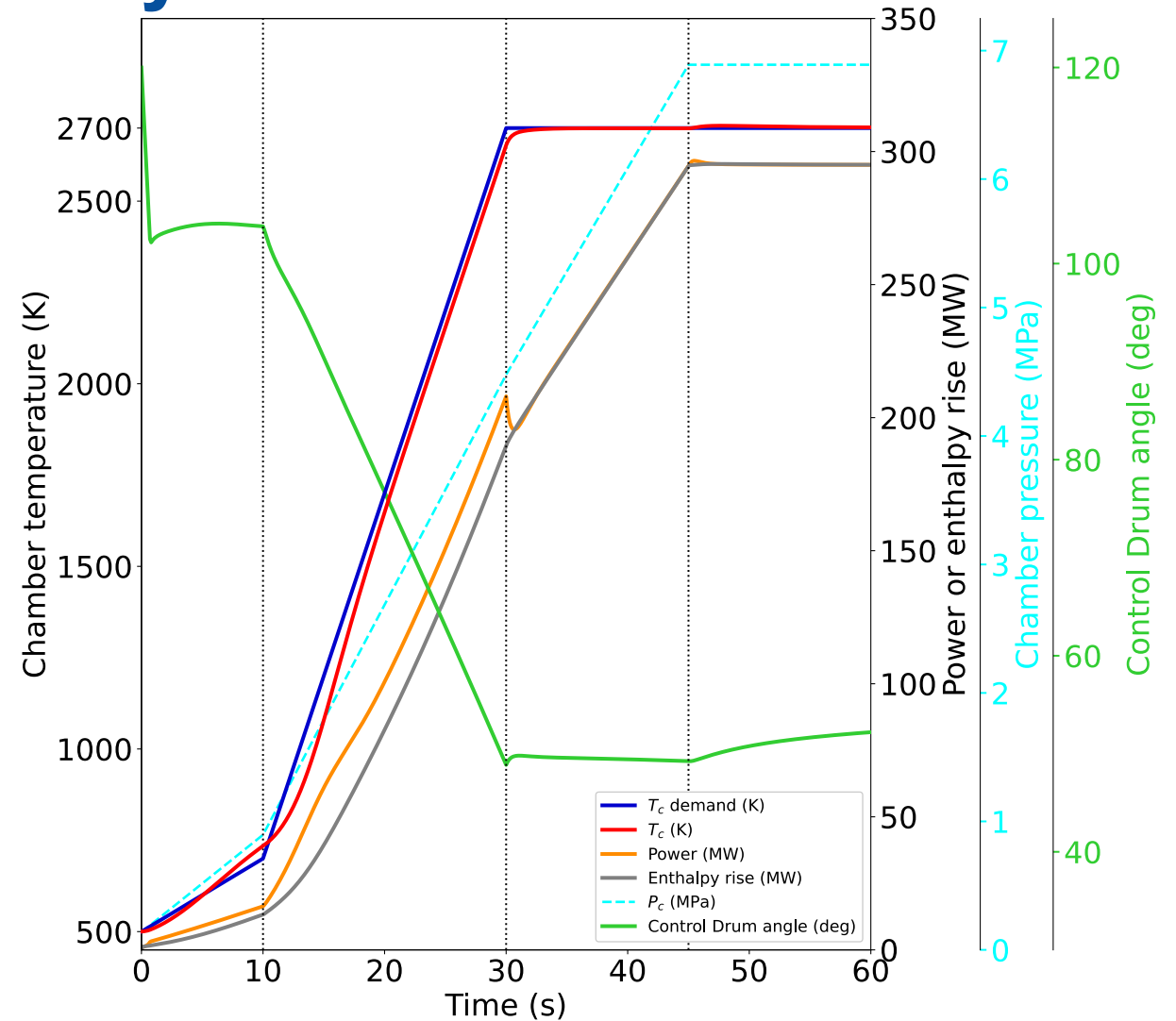
Hybrid Controller

- Use the reactivity component at early times
- Use the temperature component at later times



Hybrid Temperature-Reactivity Controller

- Initial delay/oscillations are reduced
- Derivative controller may not be practical in real system (due to noise)
- One alternative is to use time-dependent gains but how to tune them on a real system (especially near full power)?



Conclusions

- New controller proposed to limit delayed and oscillatory behavior
- But derivative term could be difficult to use in practice (noisy signal)
- Temperature delay difficult to fully overcome (unless varying gains are used for controllers)
- But difficult to determine varying gains on a real system unless it can be tested at nominal conditions
- Need to make the model more complex to further test limitations (e.g., moderator capacitance could prevent from reaching nominal temperatures within 30 s, etc.)
- Future work:
 - Incorporate into full-core multiphysics model
 - Account for instrumentation delay
 - Pressure-following controller to actuate the bypass control valve

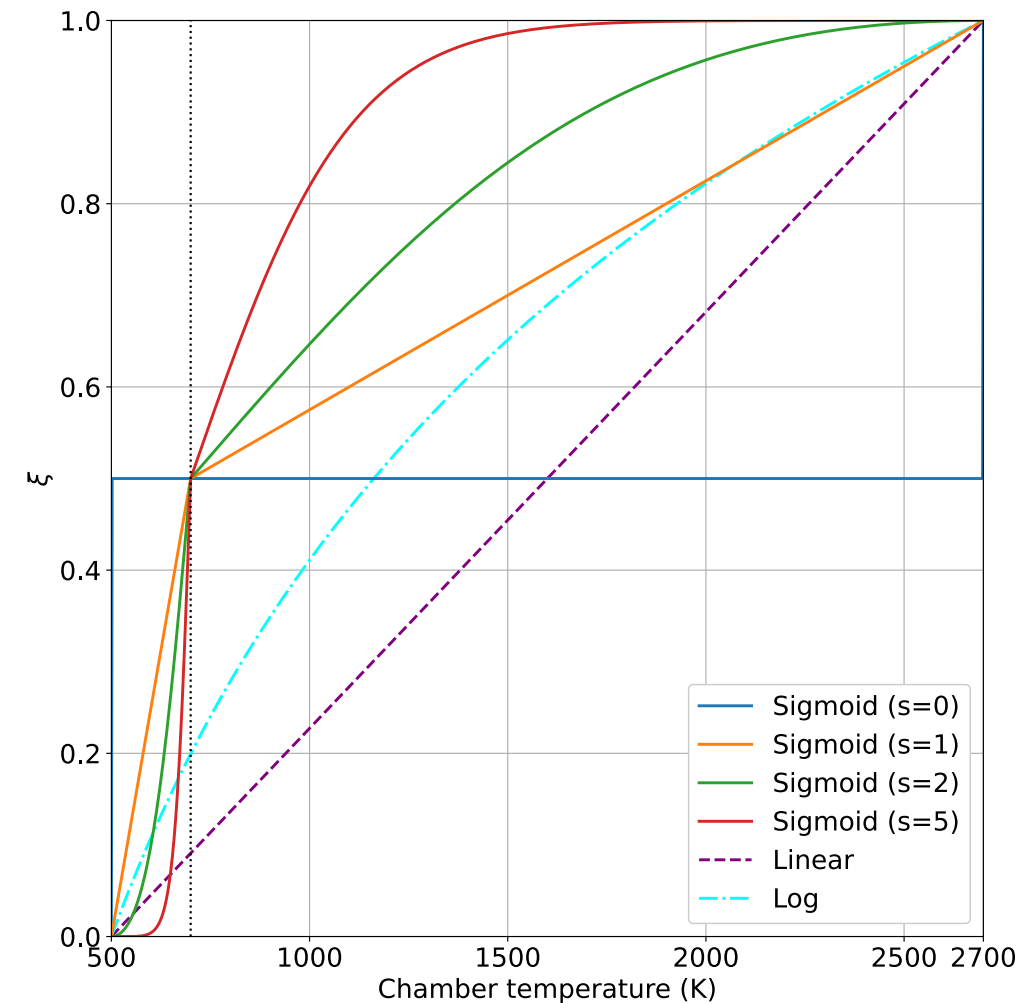


Backup Slides

Temperature-Reactivity Weighting

- Many ways of weighting:
 - Linear
 - Logarithmic
 - Sigmoid

$$\theta(t_{n+1}) = \theta_i + \sum_{k=1}^n \Delta\theta(t_k) = \theta_i + \sum_{k=1}^n \left(\xi \Delta\theta_T(t_k) + (1 - \xi) \Delta\theta_\rho(t_k) \right), \quad (5)$$



Control of NTPs

- Turbine controls pump (i.e. mass flow rate)
- Turbine power (and, in turn, mass flow rate and thrust) controlled via **BCV**, following a **chamber pressure (P_c)** signal
- Reactivity (and, in turn, the specific impulse) controlled via **control drums (CD)** and **SSCV** (adjusts moderation) following a **chamber temperature (T_c)** signal
- In practice, complicated by the fact that more flow means more moderation and more cooling so mass flow rate and temperature not independent

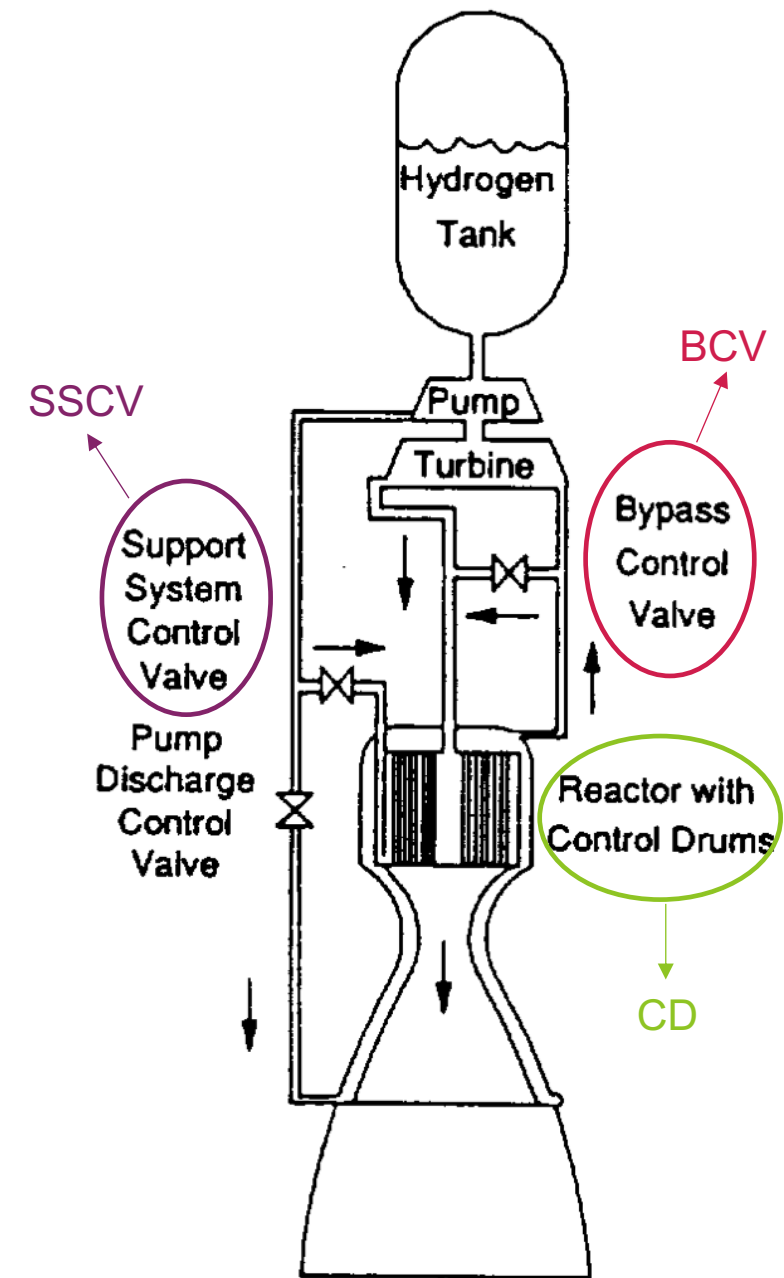
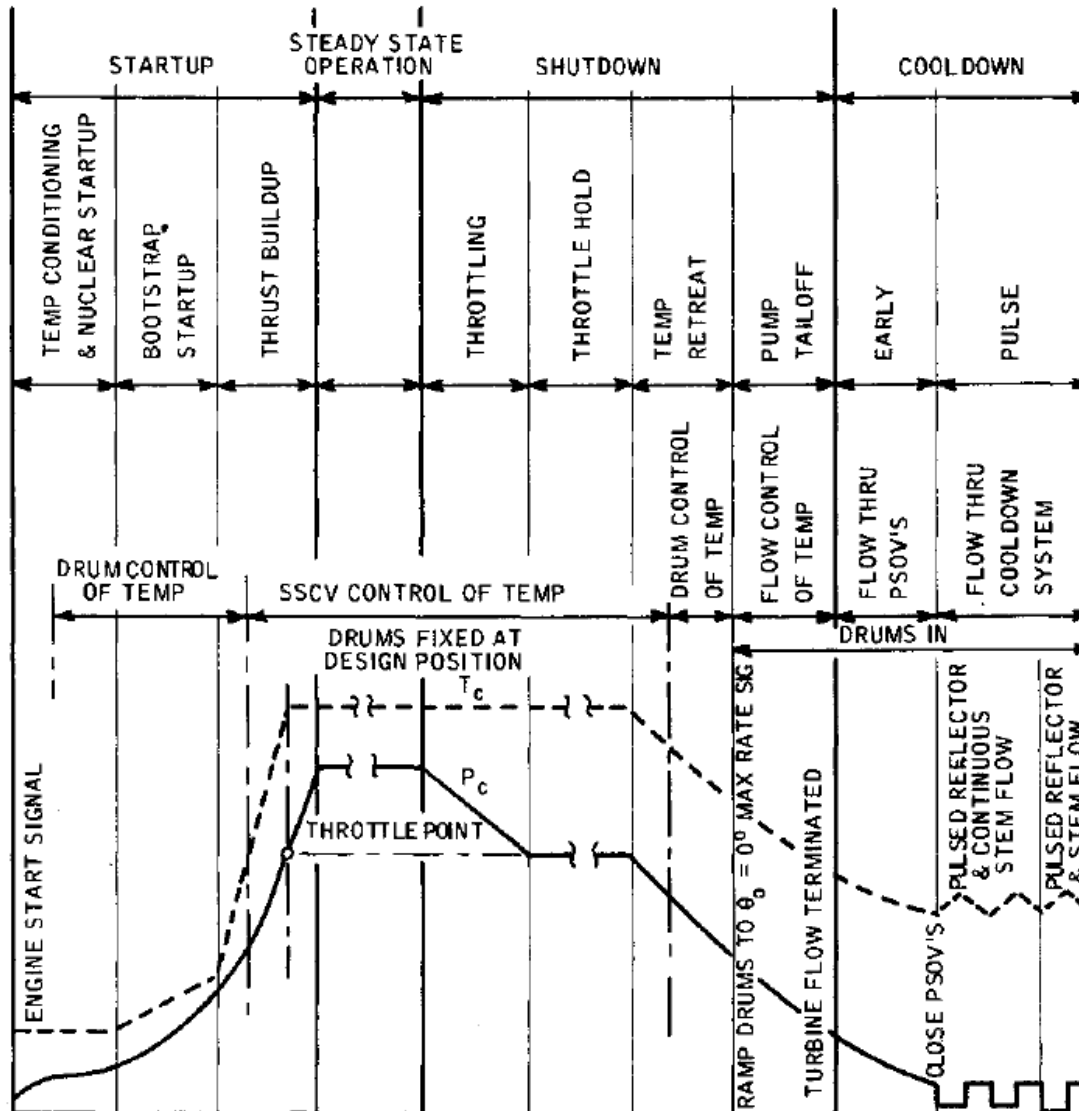


FIGURE 11. Nuclear Thermal Rocket Engine Flow Schematic.

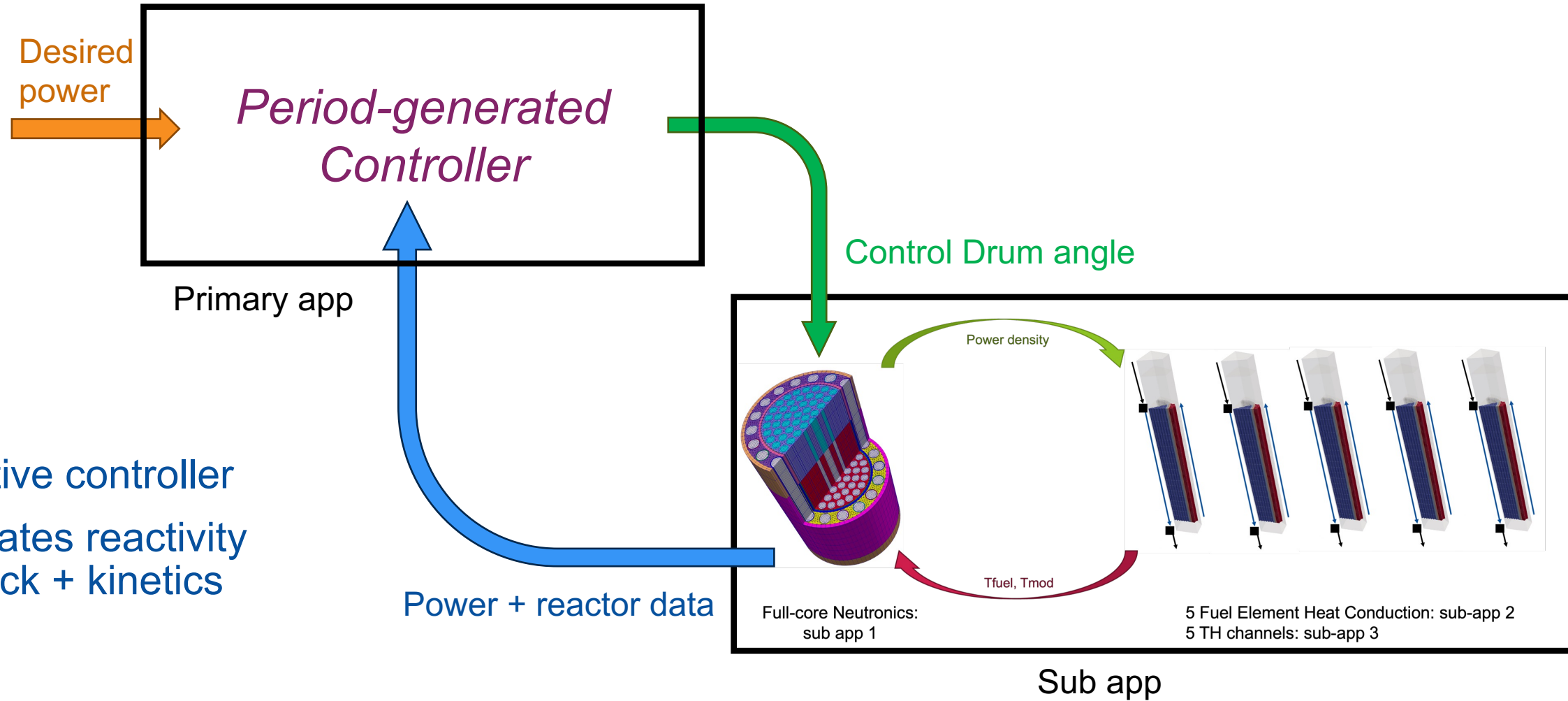
NERVA Engine Operational Phases



- Complicated start-up/shutdown phases
- Complicated control system (drum and valves)
- Chamber pressure \sim mass flow rate $\times \sqrt{T_c}$
- Chamber temperature \times mass flow rate \sim power
- Conditioning: cool pump, pre-heat core, achieve criticality, \sim 5 minutes
- Bootstrap/thrust build-up: \sim 30s
- Steady-state: 30-60 minutes
- Throttle hold: \sim 65% thrust for 1-3 min
- Cooldown: remove decay heat, e.g., with pulses

Period-Generated Control

- Predictive controller
- Anticipates reactivity feedback + kinetics



Period-generated Control of Drums

- Great initial behavior
- Little overshoot
- Requires PKE data, including:

$$\lambda'_e = \frac{\sum_{i=1}^I \lambda_i^2 C_i}{\sum_{i=1}^I \lambda_i C_i}$$

DNP concentrations

$$\rho_u(t) = \left(\frac{\partial \rho}{\partial u} \frac{\partial u}{\partial t} \right)$$

Rate of change (e.g., T_{fuel}, T_{mod}, CD angle)

Reactivity coefficients

- Depends on feedback model but small changes does not significantly degrade performance

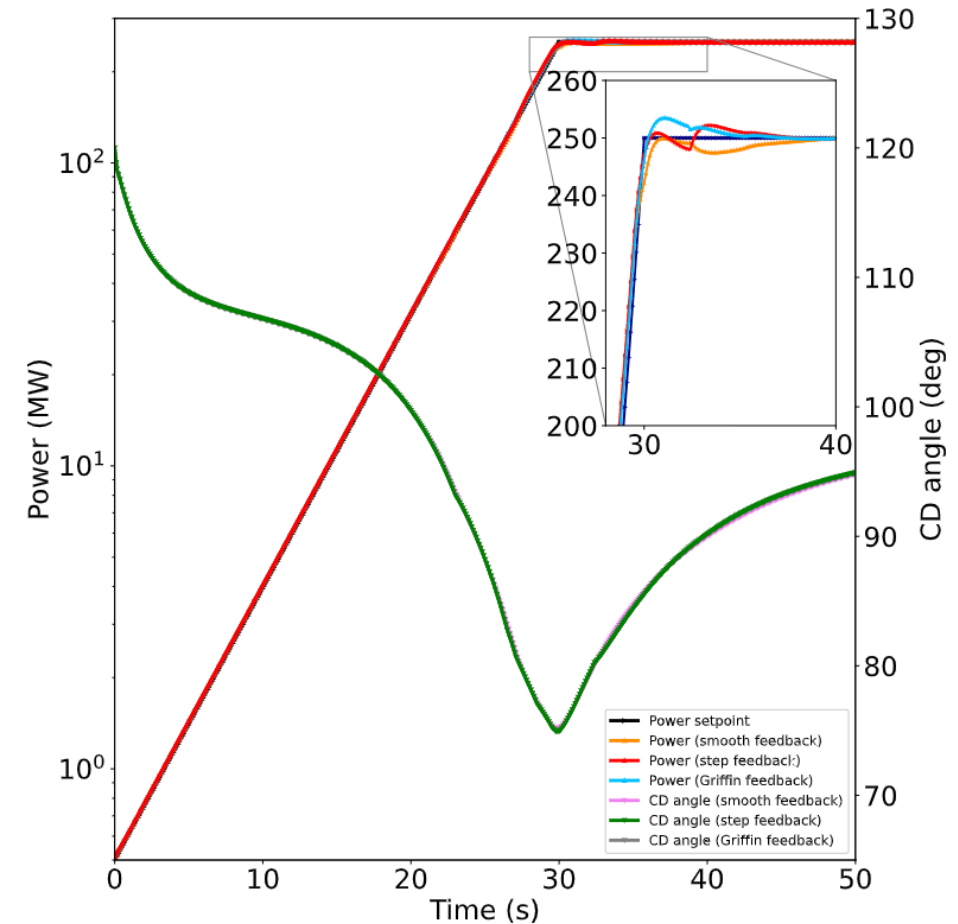


Figure 20: Evolution of the measured/demanded powers and the CD angle for the PGC under various moderator temperature feedback approximations applied to the exponential ramp-up benchmark.

How do we experimentally compute the DNP concentrations?

1. Estimate the non-fission neutron source S

2. Obtain β_{eff}, Λ from Measurement or Simulation

3. Measure $N(t)$ using neutron detector

$$4. C_k(t + \Delta) = C_k(t) + \frac{\beta_k}{\Lambda} \int_t^{t+\Delta} N(t)dt - \lambda_k \int_t^{t+\Delta} C_k(t)dt$$

$$5. \frac{\rho(t+\Delta)}{\beta_{eff}} = 1 + \frac{\Lambda}{\beta_{eff}} \frac{1}{N(t+\Delta)} \left[\frac{N(t+\Delta) - N(t)}{\Delta} - \sum_{k=1}^K \lambda_k C_k(t+\Delta) - S \right]$$

Source: M. Jaradat, TREAT Transient Analysis, C110 presentation, October 2022.

- I initially thought we would need a numerical model to compute C_i
- But can be done experimentally
- Thus, kinetics data should be doable with a real system
- However, rate of change (e.g. T_{fuel}) needed by period-generated controller would likely require a numerical model